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TABULAR PRESENTATION OF  
SUPERSONIC FLUTTER TRENDS FROM  
PISTON THEORY CALCULATIONS

WARREN H. WEATHERILL  
GARABED ZARTARIAN

MASSACHUSETTS INSTITUTE OF TECHNOLOGY

JANUARY 1958

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WRIGHT AIR DEVELOPMENT CENTER

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AIRCRAFT LABORATORY  
CONTRACT No. AF33(616)-2482  
PROJECT No. 1370

**WRIGHT AIR DEVELOPMENT CENTER  
AIR RESEARCH AND DEVELOPMENT COMMAND  
UNITED STATES AIR FORCE  
WRIGHT-PATTERSON AIR FORCE BASE, OHIO**

## FOREWORD

This note, which presents results from parameteric flutter studies on a typical section airfoil using piston theory, was prepared by the Aeroelastic and Structures Research Laboratory, Massachusetts Institute of Technology, Cambridge 39, Massachusetts, for the Aircraft Laboratory, Wright Air Development Center, Wright-Patterson Air Force Base, Ohio. The work was performed at the MIT under the direction of Professor Holt Ashley and supervised by Mr. G. Zartarian and Mr. W. H. Weatherill. The research and development work was accomplished under Air Force Contract No. AF33(616)-2482, Project No. 1370, "Aeroelasticity, Vibration and Noise", and Task No. 13478, "Theoretical Supersonic Flutter Studies". Mr. Walter J. Mykytow of the Dynamics Branch, Aircraft Laboratory is task engineer. This note contains data only and represents a part of a research program on the flutter of aircraft structures at supersonic speeds. Further reports will be published as the research continues. The basic research was started 1 July 1954 and is continuing. As part of this research WADC Technical Report 56-97, (Confidential Report - Unclassified Title) "Theoretical Studies on the Prediction of Unsteady Supersonic Airloads on Elastic Wings" has been published in two separate parts. Part I, (Unclassified Title) "Investigations on the Use of Oscillatory Supersonic Aerodynamic Influence Coefficients" which presents the studies on the use of the aerodynamic influence coefficient method, was issued in December 1955; and Part II, (Unclassified Title) "Rules for Application of Oscillatory Supersonic Aerodynamic Influence Coefficients" which presents working rules and recommendations for flutter analysis using the aerodynamic-influence-coefficient method, was issued in February 1956.

## FOREWORD (Continued)

The authors are indebted to Professor Holt Ashley and Dr. P. T. Hsu for their contributions to the research. Also, acknowledgements are due to Mrs. Ruth Lyon and her computing group for their help in making the necessary calculations, Mr. John McHugh for help in preparing the tables and figures and Miss Kathryn Roberts for typing the final manuscript.

## ABSTRACT

An extensive set of tables is presented from binary flutter calculations on the typical section airplane wing model of Theodorsen and Garrick (Ref. 1). The airloads are predicted using two-dimensional piston theory. The parameters studied include thickness as well as center of gravity position, elastic axis position, wing and aileron radii of gyration, and frequency ratio. The three binary flutter cases for which data is given are bending-torsion, bending-aileron, and torsion-aileron flutter.

## PUBLICATION REVIEW

This report has been reviewed and is approved.

FOR THE COMMANDER:

*S. P. Schwartz*  
for RANDALL D. KEATOR  
Colonel, USAF  
Chief, Aircraft Laboratory  
Directorate of Laboratories

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## LIST OF SYMBOLS

<i>a</i>	speed of sound
<i>b</i>	semi-chord of wing
<i>h</i>	vertical displacement of elastic axis as function of <i>t</i> . (See Fig. 1)
( ) <sub>F</sub>	conditions at flutter
<i>I</i> <sub>α</sub>	mass moment of inertia of wing-aileron combination about elastic axis per unit span
<i>I</i> <sub>β</sub>	mass moment of inertia of aileron about hingeline per unit span
<i>k</i>	reduced frequency of simple harmonic motion
<i>L</i> <sub>1</sub> ,--- <i>L</i> <sub>6</sub>	dimensionless coefficients defining lift on an oscillating wing
<i>m</i>	mass per unit length
<i>M</i>	free stream Mach Number
<i>M</i> <sub>1</sub> ,--- <i>M</i> <sub>6</sub>	dimensionless coefficients defining moment on an oscillating wing
<i>r</i> <sub>α</sub>	radius of gyration of wing-aileron combination referred to elastic axis ( $r_{\alpha} = \sqrt{\frac{I_{\alpha}}{M b^2}}$ )
<i>r</i> <sub>β</sub>	radius of gyration of aileron
<i>S</i> <sub>α</sub>	static unbalance of wing-aileron combination per unit span referred to the elastic axis
<i>S</i> <sub>β</sub>	static moment of aileron per unit span referred to aileron hinge
<i>t</i>	physical time
<i>U</i>	free stream velocity or flight speed
<i>w</i>	vertical component of velocity (velocity in z-direction)

LIST OF SYMBOLS (Continued)

$x_e$	position of elastic axis referred to leading edge (non-dimensionalized with respect to $2b$ )
$x_h$	position of hingeline referred to leading edge (non-dimensionalized with respect to $2b$ )
$x_a$	non-dimensional location of cg of wing-aileron combination referred to the elastic axis $(x_a = \frac{x_h}{mb})$
$x_p$	non-dimensional location of center of gravity of aileron referred to hingeline $(x_p = \frac{x_h}{m_0})$
$\alpha$	angular displacement of wing about elastic axis as function of $t$ . (See Fig. 1).
$\beta$	angular displacement of aileron measured with respect to $\alpha$ as function of time (See Fig. 1).
$\delta(x)$	thickness distribution non-dimensionalized with respect to $2b$ .
$\bar{s}$	a thickness quantity defined as $0.6 \frac{t}{b}$
$\mu$	mass density ratio defined as $\frac{\rho}{\rho_{air}}$
$\rho$	density
$\omega$	natural frequency at flutter
$\omega_h$	first natural bending frequency of wing
$\omega_e$	natural torsional frequency of wing about the elastic axis
$\omega_p$	natural torsional frequency of aileron about hingeline
$\chi$	defined as $\left(\frac{\omega_p}{\omega}\right)^2$

## SECTION 1

### PARAMETRIC STUDY OF FLUTTER AT HIGH SUPERSONIC SPEEDS

#### 1. Introduction

The objective of this report is to present the numerical results of extensive binary flutter calculations on the typical section airplane wing model of Theodorsen and Garrick (Ref. 1) with two-dimensional piston theory used for the aerodynamic terms in the flutter equations. The effects of all dimensionless system parameters on the flutter eigenvalues are included.

In order to expedite publication, no graphical presentations or interpretation of results are given herein. This is therefore an interim report, designed to make the data generally available while a more complete paper is being prepared on the same subject. The final report will contain no additional numerical information but will be devoted to interpretation of findings and discussion of ways in which the material can be used.

Piston theory is an approximate technique for estimating airloads on airfoils in unsteady motion at higher supersonic and low hypersonic speeds. It had its origins in work of Hayes (Ref. 2) and Lighthill (Ref. 3) and has been applied to aeroelastic problems in several recent publications (e.g., Refs. 4 and 5). Its use for typical section flutter analyses is desirable for several reasons. First, it yields a much simplified set of equations of motion, as compared with more conventional unsteady aerodynamic theory. In some cases the flutter determinant may even be solved in closed form. Extensive flutter calculations using piston theory can be made on any small digital computing machine, such as the Burroughs E101 which was employed in the present investigation. Second, the influence of airfoil thickness (and other nonlinear effects, if significant) can be introduced without excessive additional computational difficulty. To the authors' knowledge, this is the first parametric study of flutter which includes thickness effects. Although by no means exhaustive, the ranges of parameters covered appear to be those of general interest for the supersonic flight regime.

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WADC Technical Note.

In setting up the flutter problem for this report, a three-degree-of-freedom determinant was first derived for the system pictured in Fig. 1. Only the three sub-cases of binary flutter were calculated, however. Thus the tables list data only on bending-torsion, bending-aileron and torsion-aileron flutter of the typical section.

The flutter equations and their solution follow the pattern established by Garrick and Rubinow (Ref. 6). A symmetrical double-wedge airfoil shape has been chosen as typical of supersonic configurations.

Section 2 gives the computational details, while Section 3 discusses the manner of tabular presentation of data. In this latter connection, a few remarks are in order. Past convention has usually been to present compressible-flow-flutter boundaries on plots of dimensionless speed\* ( $U_r/b\omega_a$ ) vs. Mach number M. On such a plot, flight of a given aircraft at a given altitude is represented by a sloping straight line through the origin of coordinates. A flutter-free condition for the given altitude occurs at any M where the actual flutter curve lies above this "altitude line". This form of presentation has the disadvantage that the airspeed is contained implicitly in both the ordinate and abscissa of the stability diagram. It has been pointed out (Ref. 6) that the flutter stability boundary can equally well be presented as a curve of  $b\omega_a/a$  vs. M, where a is the speed of sound at flight altitude. Flight of a given aircraft at a given altitude is then described by a horizontal straight line; no flutter occurs if this straight line lies above the actual flutter curve. Alternatively, the flutter curve can be interpreted in terms of the torsional stiffness required for safe flight of a wing of given geometry at a given speed of sound and Mach number.

It has been pointed out that the curves for various altitudes can be brought in closer juxtaposition by multiplying the ordinate  $b\omega_a/a$  by some power of the wing-to-air density ratio  $\mu$  (thus,  $\mu^{1/2}$  can be interpreted in terms of indicated rather than true airspeed). For this reason, and because  $\mu$  and M always appear as the product  $\mu M$  in the analysis, all flutter data in the present report are given as tables of  $\mu^{1/2} b\omega_a/a$  (or  $\mu^{1/2} U_r/b\omega_a$ ) vs.  $\mu M$ , each row representing the ordinates of the stability boundary for one set of dimensionless parameters.

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\*See List of Symbols for definitions of all physical quantities.

## 2. Development of Flutter Equations

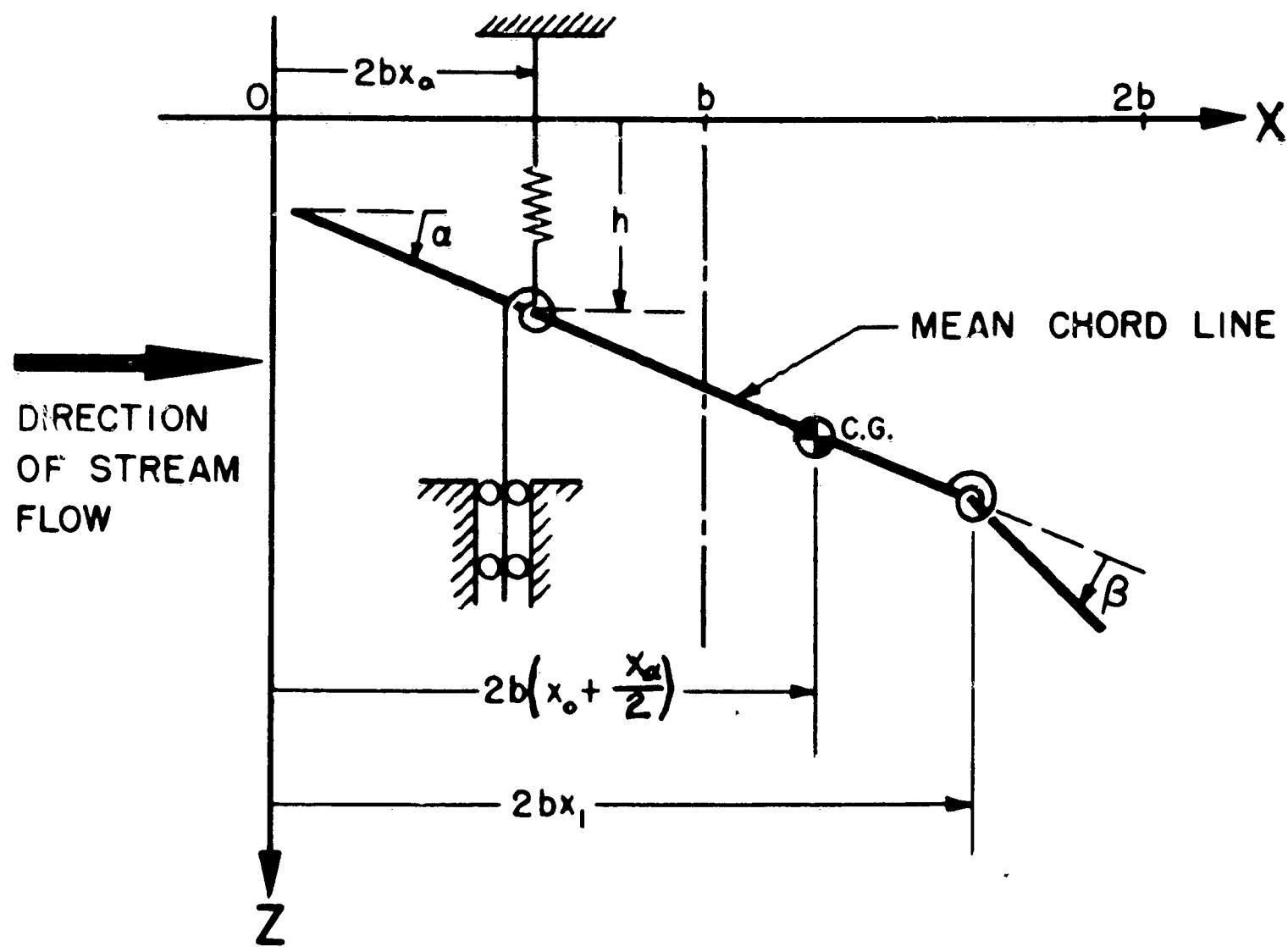
Figure 1a illustrates the two-dimensional dynamic model which forms the basis of this trend study on supersonic flutter. It is identical with the "typical section" model used by Theodorsen and Garrick (Refs. 1 and 6). This system has three degrees of freedom, described by the time-dependent quantities  $h$ ,  $\alpha$ , and  $\beta$ , which are analogous to bending, torsion and control-surface rotation, respectively, of an unswept wing or tail surface. When the equations of motion of this model in a supersonic airstream are set up, under the assumption that  $h$ ,  $\alpha$ ,  $\beta$ , vary simple-harmonically with time, there results the well-known flutter determinant (cf. Ref. 6). This complex determinant, whose vanishing supplies two characteristic equations for the flutter eigenvalues  $U_r$  and  $\omega_r$ , is of third order in the present example:

$$\begin{vmatrix} A & B & C \\ D & E & F \\ G & H & I \end{vmatrix} = 0 \quad (1)$$

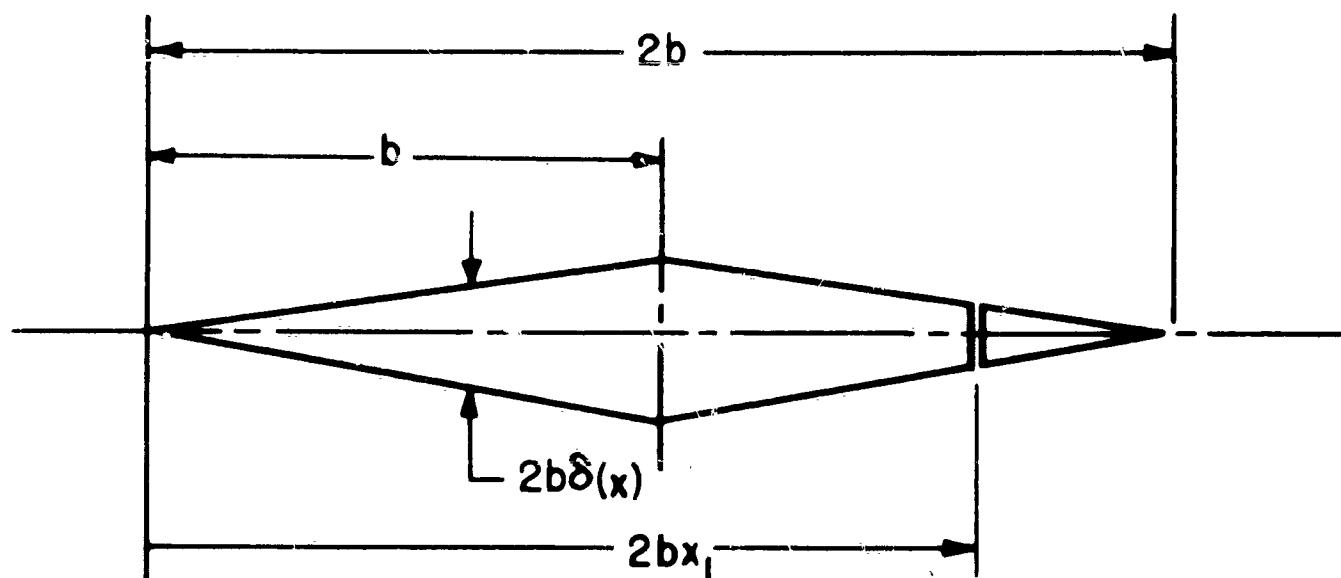
In terms of quantities defined in the List of Symbols, the elements of Eq. (1) are the following:

$$\begin{aligned} A &= \mu \left\{ \left( \frac{\omega_h}{\omega_n} \right)^2 \chi - 1 \right\} + L_1 + iL_2 \\ B &= -\mu x_\alpha + L_3 + iL_4 \\ C &= -\mu x_\beta + L_5 + iL_6 \\ D &= -\mu x_\alpha + M_1 + iM_2 \\ E &= \mu r_a^2 \left\{ \chi - 1 \right\} + N_3 + iN_4 \\ F &= -\mu [r_a^2 + 2(x_1 - x_0)x_\beta] + N_5 + iN_6 \\ G &= -\mu x_\beta + N_1 + iN_2 \\ H &= -\mu [r_a^2 + 2(x_1 - x_0)x_\alpha] + N_3 + iN_4 \\ I &= \mu r_a^2 \left\{ \left( \frac{\omega_h}{\omega_n} \right)^2 \chi - 1 \right\} + N_5 + iN_6 \end{aligned} \quad (2)$$

Here  $(L_1 + iL_2)$ , etc., are dimensionless representations of the lifts, pitching moments and control-surface hinge moments due to simple harmonic motions in the three degrees of freedom. The definitions adopted here coincide with those originally given by Garrick and Rubinow (Ref. 6). For sufficiently high supersonic



(a) DYNAMIC MODEL OF AIRFOIL SECTION



(b) GEOMETRICAL SHAPE OF AIRFOIL SECTION

Fig. 1 The Model Used For Flutter Analysis

flight Mach number  $M$ , these coefficients can be put into the relatively simple forms yielded by piston theory (Ashley and Zartarian, Ref. 5). Assuming a symmetrical double-wedge airfoil section of chord  $2b$  and thickness ratio  $\delta$ , and accounting for the second-order effect of thickness, Zartarian, Heller and Ashley (Ref. 4) give the following:

$$\begin{aligned}
 L_1 &= 0 \\
 L_2 &= \frac{1}{\mu M} \\
 L_3 &= \frac{1}{M A^2} \\
 L_4 &= \frac{1}{M A} \left\{ (1-2x_0) - \mu M \bar{\delta} \right\} \\
 L_5 &= \frac{(1-x_1)}{M A^2} \left\{ 1 - 2\mu M \bar{\delta} \right\} \\
 L_6 &= \frac{(1-x_1)^2}{M A} \left\{ 1 - 2\mu M \bar{\delta} \right\} \\
 M_1 &= 0 \\
 M_2 &= \frac{1}{M A} \left\{ (1-2x_0) - \mu M \bar{\delta} \right\} \\
 M_3 &= \frac{1}{M A^2} \left\{ (1-2x_0) - \mu M \bar{\delta} \right\} \\
 M_4 &= \frac{1}{M A} \left\{ \frac{1}{3} + (1-2x_0)^2 - 2(1-2x_0)\mu M \bar{\delta} \right\} \\
 M_5 &= \frac{(1-x_1)[(1-2x_0)+x_1]}{M A^2} \left\{ 1 - 2\mu M \bar{\delta} \right\} \\
 M_6 &= \frac{(1-x_1)^2[(1-2x_0)+\frac{2}{3}x_1+\frac{1}{3}]}{M A} \left\{ 1 - 2\mu M \bar{\delta} \right\} \\
 N_1 &= 0 \\
 N_2 &= \frac{(1-x_1)^2}{M A} \left\{ 1 - 2\mu M \bar{\delta} \right\} \\
 N_3 &= \frac{(1-x_1)^2}{M A^2} \left\{ 1 - 2\mu M \bar{\delta} \right\} \\
 N_4 &= \frac{(1-x_1)^2[(1-2x_0)+\frac{2}{3}x_1+\frac{1}{3}]}{M A} \left\{ 1 - 2\mu M \bar{\delta} \right\} \\
 N_5 &= \frac{(1-x_1)^2}{M A^2} \left\{ 1 - 2\mu M \bar{\delta} \right\} \\
 N_6 &= \frac{4(1-x_1)^3}{3 M A} \left\{ 1 - 2\mu M \bar{\delta} \right\}
 \end{aligned} \tag{3}$$

As in Ref. (1), the present report concentrates on the influence of various system parameters on solutions of the flutter determinant "Eq (1)" for the sub-cases obtained by successively suppressing each of the degrees of freedom. The determinants for these three binary flutters are

(1) Bending - torsion flutter:

$$\begin{vmatrix} A & B \\ D & E \end{vmatrix} = 0 \quad (4)$$

(2) Bending-aileron flutter:

$$\begin{vmatrix} A & C \\ G & I \end{vmatrix} = 0 \quad (5)$$

(3) Torsion-aileron flutter:

$$\begin{vmatrix} E & F \\ H & I \end{vmatrix} = 0 \quad (6)$$

It is significant that the bending-torsion sub-case can be solved explicitly for the dimensionless speed and frequency of flutter:

$$\frac{U_F}{b\omega_a} = \mu M \sqrt{\frac{x_a^2 - [(\frac{4}{\omega_a})^2 \chi - 1][\chi - 1] r_a^2}{\mu M \{(1-2x_a - \mu M \bar{\delta})[(\frac{4}{\omega_a})^2 \chi - 1] + x_a\} + (\mu M \bar{\delta})^2 - \frac{1}{3}} \chi}$$

$$\chi = \frac{r_a^2 - 2x_a(1-2x_a - \mu M \bar{\delta}) + [\frac{1}{3} + (1-2x_a)^2 - 2(1-2x_a)\mu M \bar{\delta}]}{r_a^2 + (\frac{4}{\omega_a})^2 [\frac{1}{3} + (1-2x_a)^2 - 2(1-2x_a)\mu M \bar{\delta}]} = \left(\frac{\omega_a}{\omega}\right)^2$$

These expressions display explicitly the influence of the various system parameters and combinations thereof on the eigenvalues. It is unfortunate that similar closed-form solutions cannot be written down for the other two binary flutter cases. From the computational standpoint, however, the implicit equations yielded by the bending-aileron and torsion-aileron determinants can be solved for speed and frequency with nearly equal ease.

### 3. Description of Results

The combinations of parameters used for each binary flutter solution are listed in Tables 1-3.

Tables 4 through 62 contain all the calculated results. Blank spaces indicate that no calculations were made. Asterisks indicate that careful examination of the equations shows that no

solutions exist. Dashes in the boxes mean that calculations were made and no real solutions were found.

The numbers contained in the tables, as mentioned in the Introduction, are values of  $\mu b w_s / a$  at flutter for the particular combination of parameters involved. The tables are setup with the purpose of making curves of  $\mu b w_s / a$  versus  $\mu M$  for a series of values of thickness ratio with other parameters fixed.  $\mu b w_s / a$  was chosen because, for a given configuration (values of  $b$ ,  $w_s$  and  $m$  fixed) and altitude,  $\mu b w_s / a$  is represented by a straight horizontal line in a graph of  $\mu b w_s / a$  versus  $\mu M$ . Also, a flight diagram showing the design capabilities of a particular aircraft may be superimposed on a plot of  $\mu b w_s / a$  versus  $\mu M$ . The Mach number,  $M$ , always appears in linear combination with  $\mu$ , thus  $\mu M$  was considered to be the most convenient and economical scale for the abscissa (ef. Eq. 7). Note that  $\mu$  also appears with the thickness parameter in the single combination  $\delta/\mu$ . An example of drawing a flutter boundary on a flight diagram is given in the Appendix. Although the tables are set up to be used to show trends due to thickness, the reader should have no trouble in combining any set of numbers to illustrate desired trends.

All the results were obtained for a typical section of a symmetrical double wedge airfoil section of chord  $2b$  and thickness  $2\delta b$ . For the modes used in this report (first power in  $x$  only), as shown in ref. 5, the actual profile of the wing enters the piston theory aerodynamic derivatives only in the form of the area of the airfoil section, the area of the flap, the first area moments of the wing and flap about their leading edges, and the thickness of the profile at the hinge line, all non-dimensionalized with respect to the semichord. If these parameters can be made numerically equal for two different profiles (say by adjusting the thickness parameter), then the two profiles would have the same aerodynamic derivatives. This may be done only for special systems for the binary cases including the aileron mode and for the ternary system where three or more of the above conditions must be satisfied. However, for the bending-torsion system, where only the area and first area-moment conditions must be satisfied, similarity rules may be found between all profiles having the same non-dimensional centroid of area location. For example, a doubly symmetric biconvex airfoil section with parabolic thickness distribution of maximum thickness  $2b \delta_{ac}$  will have the same bending-torsion flutter boundary as the double-wedge section of this report of maximum thickness  $2b (4\delta_{ac}/3)$ . This of course assumes that all other system parameters are identical. These various aspects will be further discussed in the final report.

**BENDING-TORSION FLUTTER**

$x_a$	$x_o$	$r_a^2$	$\delta/\mu$	$\omega_h/\omega_a$	Table No.	Page No.
0	0.35	0.09	0	0- 1.5	4	15
			0.000,5	0- 1.5		
			0.001	0- 1.5		
	0.16	0.16	0	0- 1.5	5	16
			0.000,5	0- 1.5		
			0.001	0- 1.5		
	0.25	0.25	0	0- 1.5	6	17
			0.000,5	0- 1.5		
			0.001	0- 1.5		
0.4	0.09	0.09	0	0- 1.5	7	18
			0.000,5	0- 1.5		
			0.001	0- 1.5		
	0.16	0.16	0	0- 1.5	8	19
			0.000,5	0- 1.5		
			0.001	0- 1.5		
	0.25	0.25	0	0- 1.5	9	20
			0.000,5	0- 1.5		
			0.001	0- 1.5		
0.45	0.09	0.09	0	0- 1.5	10	21
			0.000,5	0- 1.5		
			0.001	0- 1.5		
	0.16	0.16	0	0- 1.5	11	22
			0.000,5	0- 1.5		
			0.001	0- 1.5		
	0.25	0.25	0	0- 1.5	12	23
			0.000,5	0- 1.5		
			0.001	0- 1.5		

**TABLE 1**

BENDING-TORSION FLUTTER (Continued)						
$x_a$	$x_o$	$r_a^2$	$\delta/\mu$	$\omega_h/\omega_a$	Table No.	Page No.
0	0.50	0.09	0	0- 1.5	13	24
			0.000,5	0- 1.5		
			0.001	0- 1.5		
		0.16	0	0- 1.5	14	25
			0.000,5	0- 1.5		
			0.001	0- 1.5		
		0.25	0	0- 1.5	15	26
			0.000,5	0- 1.5		
			0.001	0- 1.5		
0.1	0.35	0.09	0	0- 1.5	16	27
			0.000,5	0- 1.5		
			0.001	0- 1.5		
		0.16	0	0- 1.5	17	28
			0.000,5	0- 1.5		
			0.001	0- 1.5		
		0.25	0	0- 1.5	18	29
			0.000,5	0- 1.5		
			0.001	0- 1.5		
0.4	0.4	0.09	0	0- 1.5	19	30
			0.000,5	0- 1.5		
			0.001	0- 1.5		
		0.16	0	0- 1.5	20	31
			0.000,5	0- 1.5		
			0.001	0- 1.5		
		0.25	0	0- 1.5	21	32
			0.000,5	0- 1.5		
			0.001	0- 1.5		
		0.36	0	0- 0.7	22	33

TABLE 1

BENDING-TORSION FLUTTER (Continued)						
$x_a$	$x_o$	$r_a^2$	$\delta/\mu$	$\omega_n/\omega_a$	Table No.	Page No.
0.1	0.45	0.09	0	0- 1.5	23	34
			0.000,5	0- 1.5		
			0.001	0- 1.5		
		0.16	0	0- 1.5	24	35
			0.000,5	0- 1.5		
			0.001	0- 1.5		
		0.25	0	0- 1.5	25	36
			0.000,5	0- 1.5		
			0.001	0- 1.5		
	0.36		0	0- 0.7	26	37
0.5	0.5	0.09	0	0- 1.5	27	38
			0.000,5	0- 1.5		
			0.001	0- 1.5		
		0.16	0	0- 1.5	28	39
			0.000,5	0- 1.5		
			0.001	0- 1.5		
		0.25	0	0- 1.5	29	40
			0.000,5	0- 1.5		
			0.001	0- 1.5		
	0.36		0	0- 0.7	30	41
0.55	0.09		0	0	31	42
	0.16		0	0	32	43
	0.25		0	0	33	44
	0.36		0	0	34	45

TABLE 1

BENDING-TORSION FLUTTER (Continued)						
$x_a$	$x_o$	$r_a^2$	$\delta/\mu$	$\omega_h/\omega_a$	Table No.	Page No.
0.2	0.35	0.09	0	0 - 0.7 0.3 - 0.7 0.3 - 0.7	35	46
			0.000,5			
			0.001			
		0.16	0 0.000,5 0.001	0 - 0.7 0.3 - 0.7 0.3 - 0.7	36	47
		0.25	0	0 - 0.7 0.3 - 0.7 0.3 - 0.7	37	48
			0.000,5			
			0.001			
		0.36	0	0 - 0.7	38	49
	0.40	0.09	0	0 - 0.7 0 - 0.7 0 - 0.7	39	50
			0.000,5			
			0.001			
		0.16	0 0.000,5 0.001	0 - 0.7 0 - 0.7 0 - 0.7	40	51
		0.25	0	0 - 0.7 0 - 0.7 0 - 0.7	41	52
			0.000,5			
			0.001			
		0.36	0	0 - 0.7	42	53
	0.45	0.09	0	0 - 0.7 0 - 0.7 0 - 0.7	43	54
			0.000,5			
			0.001			
		0.16	0 0.000,5 0.001	0 - 0.7 0 - 0.7 0 - 0.7	44	55
		0.25	0	0 - 0.7 0 - 0.7 0 - 0.7	45	56
			0.000,5			
			0.001			
		0.36	0	0 - 0.7	46	57

TABLE 1

## **BENDING-TORSION FLUTTER (Continued)**

BENDING-TORSION FLUTTER (Continued)

$x_a$	$x_o$	$r_a^2$	$\delta/\mu$	$\omega_h/\omega_a$	Table No.	Page No.
0.2	0.50	0.09	0	0- 0.7	47	58
			0.000,5	0- 0.7		
			0.001	0- 0.7		
		0.16	0	0- 0.7	48	59
0.000,5	0- 0.7					
0.001	0- 0.7					
0.25	0	0- 0.7	49	60		
	0.000,5	0- 0.7				
	0.001	0- 0.7				
0.36	0	0- 0.7	50	61		

TABLE 1

BENDING-AILERON							
$x_1$	$r\beta^2$	$x_\beta$	$\delta/\mu$	$\mu_M$	$\frac{\omega_\beta}{\omega_h}$	Table No.	Page No.
0.8	0.001,96	0	0 0.001	40-400	0- 1.0	51	62
		0.01	0 0.001	40-400	0- 1.0	52	63
		0.014	0 0.001	40-400	0- 1.0	53	64
0.8	0.003,24	0	0 0.001	40- 400	0- 1.0	54	65
		0.01	0 0.001	40- 400	0- 1.0	55	66
		0.014	0 0.001	40- 400	0- 1.0	56	67

TABLE 2

### **TORSION-AILERON**

TORSION-AILERON							
$x_1$	$\beta^2$	$x_\beta$	$\delta/\mu$	$\mu M$	$\frac{\omega_\beta}{\omega_a}$	Table No.	Page No.
0.8	0.001,96  $x_o=0.4$ $r_a^2=0.36$	0	0 0.001	40- 400	0- 1.0	57	68
		0.01	0 0.001	40- 400	0- 1.0	58	69
		0.014	0 0.001	40- 400	0- 1.0	59	70
0.8	0.003,24  $x_o=0.4$ $r_a^2=0.36$	0	0 0.001	40- 400	0- 1.0	60	71
		0.01	0 0.001	40- 400	0- 1.0	61	72
		0.014	0 0.001	40- 400	0- 1.0	62	73

**TABLE 3**

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$\frac{\omega_h}{\omega_n}$	$\mu_M$	$\mu_L$	40	60	80	100	120	140	160	180	200	240	320	400	500	600
0	0	0.0005 0.001	*	*	*	*	*	*	*	*	*	*	*	*	*	*
0.3	0	0.0005 0.001	*	*	*	*	*	*	*	*	*	*	*	*	*	23.870
0.5	0	0.0005 0.001	*	*	*	*	*	*	*	*	*	*	*	*	*	25.994
0.7	0	0.0005 0.001	*	*	*	*	*	*	*	*	*	*	*	*	*	27.656
0.8	0	0.0005 0.001	-	-	-	-	-	-	-	-	-	-	-	-	-	39.134
0.9	0	0.0005 0.001	-	-	-	-	-	-	-	-	-	-	-	-	-	52.559
1.0	0	0.0005 0.001	*	*	*	*	*	*	*	*	*	*	*	*	*	*
1.1	0	0.0005 0.001	9.405 8.247 6.929	21.758 20.530 19.245	29.298 37.581 25.773	40.352 37.366 34.140	52.756 54.345 44.200	62.753 54.368 44.252	74.012 60.843 43.201	83.771 64.867 35.244	94.565 67.041 -	104.246 66.228 -				
1.3	0	0.0005 0.001	12.243 11.928 11.605	16.342 15.783 15.205	19.601 18.750 21.629	24.870 23.311 21.858	31.145 28.250 24.972	36.352 31.823 26.386	42.310 35.153 25.659	47.527 37.221 21.398	53.335 38.301 -	58.569 37.787 -				
1.5	0	0.0005 0.001	9.800 9.575 9.349	12.678 12.271 11.850	15.013 14.390 13.736	18.834 17.685 16.446	23.425 21.286 18.863	27.254 23.901 19.878	31.646 26.343 19.319	35.499 27.858 16.167	39.793 28.644 -	43.668 28.253 -				
	$X_a = 0$															$r_a^2 = 0.09$

(See pages 6 and 7 for explanation of dashes and asterisks)

TABLE 4

$\frac{\mu_{be}}{a}$  FOR BENDING-TORSION FLUTTER

$\frac{C_1}{C_2}$	$\delta/\mu$	$\mu M$	40	60	80	120	180	240	320	400	500	600
0	0.0005 0.001	0	*	*	*	*	*	*	*	*	*	*
0.3	0.0005 0.001	0	*	*	*	*	*	*	*	*	*	*
0.5	0.0005 0.001	0	*	*	*	*	*	*	*	*	*	*
0.7	0.0005 0.001	0	*	*	*	*	*	*	*	*	*	*
0.8	0.0005 0.001	0	-	-	-	-	-	-	-	-	-	*
0.9	0.0005 0.001	0	-	-	-	-	-	-	-	-	-	*
1.0	0.0005 0.001	0	*	*	*	*	*	*	*	*	*	*
1.1	0.0005 0.001	0	14.786 14.268 13.734	21.557 20.713 19.836	26.660 25.411 24.096	34.683 32.445 30.016	44.058 39.952 35.255	51.762 45.365 37.571	60.527 50.440 36.743	68.175 53.649 30.531	76.669 55.444 -	84.312 54.887 -
1.3	0.0005 0.001	0	10.807 10.573 10.334	13.845 13.424 12.987	16.327 15.682 15.003	20.404 19.217 17.929	25.318 23.106 20.579	29.422 25.953 21.739	34.135 28.640 21.223	38.273 30.339 17.872	42.886 31.275 -	47.050 30.940 -
1.5	0.0005 0.001	0	8.361 8.192 8.019	10.547 10.239 9.919	12.352 11.878 11.379	15.338 14.462 13.511	18.954 17.318 15.449	21.984 19.415 16.295	25.468 21.395 15.903	28.531 22.648 13.423	31.948 23.335 -	35.034 23.083 -

TABLE 5  $\frac{\mu b w_s}{a}$  FOR BENDING-TORSION FLUTTER  
WADC TN 57-310 16

TABLE 6  $\frac{\mu D \omega_a}{\alpha}$  FOR BENDING-TORSION FLUTTER  
WADC TN 57-310 17

$\frac{(\text{d}h)}{\text{d}x}$	$\frac{8}{\mu} \cdot \frac{\mu M}{\text{h}}$	40	60	80	120	180	240	320	400	500	600	
0	0.0005 0.001	*	*	*	*	*	*	*	*	*	*	
0.3	0.0005 0.001	*	-	*	-	*	*	*	*	*	*	
0.5	0.0005 0.001	*	-	*	-	*	*	*	*	*	*	
0.7	0.0005 0.001	*	-	*	-	*	*	*	*	*	*	
0.8	0.0005 0.001	*	-	*	-	*	*	*	*	*	*	
0.9	0.0005 0.001	*	-	*	-	*	*	*	*	*	*	
1.0	0.0005 0.001	*	-	*	-	*	*	*	*	*	*	
1.1	0.0005 0.001	-	12.672 10.037 6.451	20.573 17.700 14.293	30.799 26.321 20.921	41.672 33.872 23.540	50.245 38.246 19.570	59.793 40.791 -	68.014 40.128 -	77.066 34.311 -	85.161 18.088 -	
1.3	0.0005 0.001	0	9.085 8.605 8.097	12.747 11.951 11.098	15.570 14.387 13.094	20.058 17.926 15.486	25.340 21.397 16.450	29.698 23.490 14.600	34.666 24.697 -	39.006 24.296 -	43.831 21.306 -	48.175 13.792 -
1.5	0.0005 0.001	0	7.606 7.284 6.948	10.099 9.538 8.941	12.088 11.240 10.318	15.309 13.760 11.996	19.151 16.263 12.665	22.341 17.779 11.319	25.993 18.652 12.558	29.191 18.349 -	32.753 16.153 -	35.964 10.715 -
											$X_0 = 0.4$	
											$r_a^2 = 0.09$	
											$X_a = 0$	

TABLE 7  $\frac{\mu b \omega_a}{\sigma}$  FOR BENDING-TORSION FLUTTER  
WADC TN 57-310 18

$\left(\frac{q}{\rho A}\right)$	$\delta/\mu$	$\mu_M$	40	60	80	120	180	240	320	400	500	600
0	0.0005 0.001	0 0.0005 0.001	*	*	*	*	*	*	*	*	*	*
0.3	0.0005 0.001	0 0.0005 0.001	*	-	*	*	*	*	*	*	*	*
0.5	0.0005 0.001	0 0.0005 0.001	*	-	*	*	-	*	-	*	-	*
0.7	0.0005 0.001	0 0.0005 0.001	*	-	*	*	-	*	-	*	-	*
0.8	0.0005 0.001	0 0.0005 0.001	*	-	*	-	-	-	*	-	*	*
0.9	0.0005 0.001	0 0.0005 0.001	*	-	*	-	-	-	-	-	-	-
1.0	0.0005 0.001	0 0.0005 0.001	*	*	*	*	*	*	*	*	*	*
1.1	0.0005 0.001	0 0.0005 0.001	9.061 8.032 6.855	15.880 14.540 13.065	20.549 18.673 16.580	27.611 24.374 20.589	35.673 29.309 22.250	42.223 33.066 19.405	49.629 34.983 -	56.066 34.459 -	63.196 29.996 -	69.599 18.240 -
1.3	0.0005 0.001	0 0.0005 0.001	8.522 8.185 7.834	11.152 10.562 9.933	13.272 12.377 11.402	16.723 15.084 13.209	20.855 17.792 13.949	24.294 19.448 12.515	28.236 20.419 3.308	31.691 20.117 -	35.540 17.763 -	39.011 11.879 -
1.5	0.0005 0.001	0 0.0005 0.001	6.726 6.489 6.242	8.591 8.166 7.715	10.118 9.468 8.762	12.630 11.430 10.061	15.660 13.407 10.590	18.192 14.618 10.540	21.101 15.328 15.204	23.654 15.102 -	26.502 13.367 -	29.073 9.067 -
$X_a = 0$											$r^2 = 0.16$	

TABLE 8  
WADC TN 57-310

$\frac{\mu_{be}}{d}$  FOR BENDING-TORSION FLUTTER

TABLE 9

WADC TN 57-310

# $\frac{\mu b \omega_a}{\sigma}$ FOR BENDING-TORSION FLUTTER

$\frac{\omega_b}{\omega_a}$	$\mu M$	$\delta/\mu$	40	60	80	120	180	240	320	400	500	600
0	0	-	*	-	*	*	*	*	*	*	*	*
	0.0005	0.001	*	-	-	-	-	-	-	-	-	-
0.3	0	-	*	-	*	*	*	*	*	*	*	*
	0.0005	0.001	*	-	-	-	-	-	-	-	-	-
0.5	0	-	*	-	*	*	*	*	*	*	*	*
	0.0005	0.001	*	-	-	-	-	-	-	-	-	-
0.7	0	-	*	-	*	*	*	*	*	*	*	*
	0.0005	0.001	*	-	-	-	-	-	-	-	-	-
0.8	0	-	*	-	*	*	*	*	*	*	*	*
	0.0005	0.001	*	-	-	-	-	-	-	-	-	-
0.9	0	-	*	-	*	*	*	*	*	*	*	*
	0.0005	0.001	*	-	-	-	-	-	-	-	-	-
1.0	0	-	*	-	*	*	*	*	*	*	*	*
	0.0005	0.001	*	-	-	-	-	-	-	-	-	-
1.1	0	-	*	-	*	*	*	*	*	*	*	*
	0.0005	0.001	*	-	-	-	-	-	-	-	-	-
1.3	0	-	*	-	*	*	*	*	*	*	*	*
	0.0005	0.001	*	-	-	-	-	-	-	-	-	-
1.5	0	-	*	-	*	*	*	*	*	*	*	*
	0.0005	0.001	*	-	-	-	-	-	-	-	-	-

$$r_a^2 = 0.09$$

$$X_a = 0.45$$

$$X_a = 0$$

TABLE 10  
WADC TN 57-310

$\frac{\mu b \omega_a}{\sigma}$  FOR BENDING-TORSION FLUTTER

$\frac{\mu M}{\mu^2 \alpha}$	$\theta/\mu$	$\mu_M$	40	60	80	120	180	240	320	400	500	600
0	0	*	*	*	*	*	*	*	*	*	*	*
	0.0005	-	-	-	-	-	-	-	-	8.489	15.268	21.291
0.3	0	*	*	*	*	*	*	*	*	23.172	31.234	39.344
	0.0005	-	-	-	-	-	3.235	9.830	16.665	-	-	-
0.5	0	*	*	*	*	*	*	*	*	8.844	15.975	22.292
	0.0005	-	-	-	-	-	3.243	10.258	17.444	24.274	32.731	41.236
0.7	0	*	*	*	*	*	*	*	*	9.597	17.520	24.510
	0.0005	-	-	-	-	-	3.151	11.178	19.148	26.694	36.025	45.403
0.8	0	*	*	*	*	*	*	*	*	11.154	20.993	29.549
	0.0005	-	-	-	-	-	1.856	13.153	23.002	32.228	43.594	54.999
0.9	0	*	*	*	*	*	*	*	*	12.486	24.589	34.900
	0.0005	-	-	-	-	-	-	15.008	27.037	38.134	51.743	65.367
1.0	0	*	*	*	*	*	*	*	*	-	13.350	32.128
	0.0005	-	-	-	-	-	-	-	-	51.557	70.640	46.900
1.1	0	*	*	*	*	*	*	*	*	-	-	-
	0.0005	-	-	-	-	-	-	-	-	-	89.656	-
1.3	0	*	*	*	*	*	*	*	*	-	-	-
	0.0005	-	-	-	-	-	3.565	9.999	16.568	23.158	28.250	45.562
1.5	0	*	*	*	*	*	*	*	*	7.496	-	-
	0.0005	-	-	-	-	-	-	-	-	-	-	-
$X_a = 0$												
$r_a^2 = 0.16$												

TABLE 11

$\frac{\mu b \omega}{\alpha}$  FOR BENDING-TORSION FLUTTER

WADC TN 57-310

$(\frac{\theta h}{\omega^2})$	$\delta/\mu$	$\mu M$	40	60	80	100	120	140	160	180	200	240	320	400	500	600
0	0.0005 0.001	0 -	*	*	*	*	*	*	*	-	2.819	8.577	14.565	20.287	27.406	34.603
0.3	0.0005 0.001	0 -	*	*	*	*	*	*	*	-	2.858	8.961	15.252	21.256	28.722	36.269
0.5	0.0005 0.001	0 -	*	*	*	*	*	*	*	-	2.877	9.790	16.755	23.384	31.619	39.938
0.7	0.0005 0.001	0 -	*	*	*	*	*	*	*	-	2.395	11.606	20.173	28.260	38.281	48.391
0.8	0.0005 0.001	0 -	*	*	*	*	*	*	*	-	13.392	23.78	-	-	-	-
0.9	0.0005 0.001	0 -	*	*	*	*	*	*	*	-	16.539	31.769	45.463	62.185	78.958	57.532
1.0	0.0005 0.001	0 -	*	*	*	*	*	*	*	-	*	*	*	*	*	*
1.1	0.0005 0.001	0 -	*	*	*	*	*	*	*	-	7.644	11.147	15.998	21.294	25.514	30.237
1.3	0.0005 0.001	0 -	*	*	*	*	*	*	*	-	4.902	7.930	10.823	11.802	9.460	-
1.5	0.0005 0.001	0 -	*	*	*	*	*	*	*	-	6.636	8.005	10.205	12.816	14.979	17.450

TABLE 12  
WADC TN 57-310

$\mu_{\text{b} \alpha}$  FOR BENDING-TORSION FLUTTER

$$X_a = 0 \quad X_0 = 0.45 \quad r_a^2 = 0.25$$

$(\frac{\omega h}{\omega_a})$	$\mu_M$	$\delta/\mu$	40	60	80	120	180	240	320	400	500	600
0	0	*	1.439	3.247	4.733	7.502	11.511	15.466	20.710	25.939	32.465	*
	0.0005	-	2.975	5.079	7.037	10.830	16.425	21.983	29.374	36.753	45.970	38.984
	0.001	*	-	*	*	*	*	*	*	*	*	55.183
0.3	0	*	-	3.030	4.713	7.710	11.967	16.140	21.656	27.149	33.999	*
	0.0005	-	2.707	5.094	7.213	11.248	17.151	22.996	30.757	38.502	48.171	40.840
	0.001	*	*	*	*	*	*	*	*	*	*	57.835
0.5	0	*	-	2.057	4.477	8.077	12.920	17.586	23.714	29.794	37.364	*
	0.0005	-	4.960	7.500	12.112	18.714	25.202	33.788	42.343	53.014	63.672	44.916
	0.001	*	*	*	*	*	*	*	*	*	*	*
0.7	0	*	-	3.010	1.519	8.296	14.781	20.688	28.293	35.769	45.030	*
	0.0005	-	-	-	-	7.463	13.746	22.108	30.141	40.678	51.128	64.134
	0.001	*	*	*	*	*	*	*	*	*	*	54.243
0.8	0	*	-	-	-	5.389	6.891	16.117	23.599	32.944	42.005	*
	0.0005	-	-	-	-	14.773	25.377	35.215	47.957	60.512	76.095	64.210
	0.001	*	*	*	*	*	*	*	*	*	*	91.607
0.9	0	*	-	-	-	-	-	14.328	27.756	42.137	55.385	*
	0.0005	-	-	-	-	-	-	30.677	45.595	64.045	81.868	71.319
	0.001	*	*	*	*	*	*	*	*	*	*	86.906
1.0	0	*	-	*	*	*	*	-	-	-	-	*
	0.0005	-	*	*	*	*	*	-	-	-	-	*
	0.001	*	*	*	*	*	*	-	-	-	-	*
1.1	0	*	-	*	*	*	*	-	-	-	-	*
	0.0005	-	*	*	*	*	*	-	-	-	-	*
	0.001	*	*	*	*	*	*	-	-	-	-	*
1.3	0	*	-	*	*	*	*	-	-	-	-	*
	0.0005	-	*	*	*	*	*	-	-	-	-	*
	0.001	*	*	*	*	*	*	-	-	-	-	*
1.5	0	*	-	*	*	*	*	-	-	-	-	*
	0.0005	-	*	*	*	*	*	-	-	-	-	*
	0.001	*	*	*	*	*	*	-	-	-	-	*
$X_0 = 0.5$												$r_a^2 = 0.09$
$X_a = 0$												

TABLE 13  
WADC TN 57-310

$\frac{\mu b \omega_a}{a}$  FOR BENDING-TORSION FLUTTER

$(\frac{\omega_h}{\omega_a})$	$\mu_M$	$\mu_M$	40	60	80	120	180	240	320	400	500	600
0	0.0005	0	*	*	*	*	*	*	*	*	*	*
	0.001	0	1.165	2.629	3.832	6.074	9.320	12.522	16.768	21.001	26.284	31.563
0.3	0.0005	0	*	*	*	*	*	*	*	*	*	*
	0.001	0	0.678	2.561	3.886	6.286	9.717	13.088	17.549	21.993	27.536	33.073
0.5	0.0005	0	*	*	*	*	*	*	*	*	*	*
	0.001	0	-	1.876	2.234	3.919	6.706	10.565	14.315	19.256	24.167	30.286
0.7	0.0005	0	*	*	*	*	*	*	*	*	*	*
	0.001	0	-	-	3.913	3.303	7.382	12.351	17.024	23.106	29.115	36.578
0.8	0.0005	0	*	*	*	*	*	*	*	*	*	*
	0.001	0	-	-	0.451	6.599	12.937	21.118	28.916	39.109	49.201	51.992
0.9	0.0005	0	*	*	*	*	*	*	*	*	*	*
	0.001	0	-	-	-	-	-	-	-	-	-	-
1.0	0.0005	0	*	*	*	*	*	*	*	*	*	*
	0.001	0	-	-	-	-	-	-	-	-	-	-
1.1	0.0005	0	*	*	*	*	*	*	*	*	*	*
	0.001	0	-	-	-	-	-	-	-	-	-	-
1.3	0.0005	0	*	*	*	*	*	*	*	*	*	*
	0.001	0	-	-	-	-	-	-	-	-	-	-
1.5	0.0005	0	*	*	*	*	*	*	*	*	*	*
	0.001	0	-	-	-	-	-	-	-	-	-	-

$$r_a^2 = 0.16$$

$$X_a = 0$$

$$X_0 = 0.5$$

TABLE 14

$\frac{\mu b \omega}{c}$  FOR BENDING-TORSION FLUTTER

WADC TN 57-310

**TABLE 15**       $\frac{P_{\text{max}}}{d}$       **FOR BENDING-TORSION FLUTTER**

WADC TN 57-310

$\frac{U_h}{\mu_1}$	$\frac{\mu_1}{\mu_2}$	40	60	80	120	180	240	320	400	500	600
0	0.0005 0.001	*	*	*	*	*	*	*	*	*	*
0.3	0.0005 0.001	*	*	*	*	*	*	*	*	*	*
0.5	0.0005 0.001	*	*	*	*	*	*	*	*	*	*
0.7	0.0005 0.001	7.277 7.890	9.899 10.904	12.152 13.594	16.154 18.554	21.576 25.537	26.674 32.276	33.220 41.069	39.604 49.729	47.446 60.425	55.187 71.012
0.8	0.0005 0.001	10.657 11.122	13.593 14.407	15.999 17.219	19.959 22.122	24.739 28.567	28.734 34.454	33.322 41.834	37.351 48.873	41.846 57.385	45.903 65.671
0.9	0.0005 0.001	13.475 13.841	16.993 17.640	19.899 20.873	24.705 26.442	30.528 33.615	35.404 40.025	41.016 47.889	45.950 55.226	51.448 63.992	56.415 72.357
1.0	0.0005 0.001	15.099 15.373	18.941 19.424	22.125 22.851	27.405 28.693	33.814 36.086	39.188 42.564	45.373 50.346	50.812 57.470	56.883 65.713	62.366 73.385
1.1	0.0005 0.001	15.616 15.797	19.530 19.847	22.782 23.253	28.181 29.005	34.740 36.166	40.244 42.323	46.582 49.562	52.156 56.031	58.379 63.315	64.000 69.881
1.3	0.0005 0.001	14.650 14.694	18.263 18.330	21.271 21.361	26.274 26.406	32.358 32.531	37.468 43.442	43.353 48.419	48.530 53.756	54.312 58.284	
1.5	0.0005 0.001	12.879 12.851	16.057 16.004	18.687 18.596	23.064 22.871	28.391 27.985	32.866 32.173	38.021 36.825	42.557 40.710	47.623 52.200	

$r_a^2 = 0.09$

$X_0 = 0.35$

$r_a^2 = 0.09$

TABLE 16  $\frac{\mu_b \omega_a}{\sigma}$  FOR BENDING-TORSION FLUTTER

WADC TN 57-310

$\frac{\Omega_h}{\omega_n}$	$\frac{M}{\mu M}$	40	60	80	120	180	240	320	400	500	600
0	0	*	*	*	*	*	*	*	*	*	*
	0.0005	*	*	*	*	*	*	*	*	*	*
0.3	0	*	*	*	*	*	*	*	*	*	*
	0.0005	*	*	*	*	*	*	*	*	*	*
0.5	0	*	-	-	-	-	-	-	-	-	*
	0.0005	-	-	-	-	-	-	-	-	-	*
0.7	0	*	*	*	*	*	*	*	*	*	*
	0.0005	2.980	5.128	6.869	9.967	14.264	18.400	23.806	29.147	35.770	42.353
0.8	0	8.269	10.679	12.638	15.844	19.699	22.914	26.603	29.838	33.446	36.701
	0.0005	8.758	11.522	13.890	18.042	23.555	28.637	35.054	41.216	48.691	55.983
0.9	0	12.970	16.373	19.182	23.826	29.450	34.159	39.578	44.341	49.654	54.457
	0.0005	13.313	16.978	20.089	25.438	32.305	38.422	45.911	52.896	61.130	69.007
1.0	0	16.208	20.298	23.693	29.327	36.167	41.906	48.513	54.322	60.807	66.665
	0.0005	16.415	20.662	24.235	30.281	37.838	44.372	52.117	59.116	67.119	74.496
1.1	0	17.062	21.284	24.797	30.637	37.740	43.703	50.572	56.613	63.360	69.454
	0.0005	17.128	21.392	24.950	30.887	38.137	44.236	51.249	57.378	64.135	70.111
1.3	0	14.578	18.114	21.064	25.979	31.964	36.993	42.789	47.888	53.585	58.731
	0.0005	14.505	17.971	20.838	25.548	31.143	35.694	40.723	44.912	49.267	52.836
1.5	0	11.723	14.539	16.892	20.815	25.596	29.614	34.247	38.323	42.877	46.992
	0.0005	11.628	14.359	16.611	20.288	24.610	28.075	31.831	34.882	37.943	40.321

$r_a^2 = C \cdot 15$

$X_0 = 0.35$

$X_a = 0.1$

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TABLE 17 FOR BENDING-TORSION FLUTTER

$\frac{2h}{\mu}$	$\delta/\mu$	40	60	80	100	120	140	160	180	200	240	320	400	500	600
0	0.0005	*	*	*	*	*	*	*	*	*	*	*	*	*	*
0	0.001	*	*	*	*	*	*	*	*	*	*	*	*	*	*
0.3	0.0005	*	*	*	*	*	*	*	*	*	*	*	*	*	*
0.3	0.001	*	*	*	*	*	*	*	*	*	*	*	*	*	*
0.5	0.0005	*	-	*	*	*	*	*	-	*	-	*	*	*	*
0.5	0.001	-	-	-	-	-	-	-	-	-	-	-	-	-	-
0.7	0.0005	*	*	*	*	*	*	*	*	*	*	*	*	*	*
0.7	0.001	-	-	2.812	5.057	8.819	14.084	19.229	26.031	32.811	41.279	49.754	56.534	63.396	69.563
0.8	0.0005	0	6.315	8.318	9.925	12.536	15.656	18.249	21.221	23.823	26.723	29.337	32.842	36.618	40.118
0.8	0.001	0	6.856	9.230	11.264	14.858	19.685	24.185	29.918	35.462	42.223	48.842	52.472	56.209	60.629
0.9	0.0005	0	12.051	15.798	18.516	23.008	28.446	33.001	38.241	42.843	47.979	52.617	57.561	62.561	67.954
0.9	0.001	0	12.824	16.364	19.365	24.513	31.105	36.961	44.099	50.741	58.561	65.967	71.653	77.653	83.453
1.0	0.0005	0	17.181	21.488	25.065	31.005	38.222	44.278	51.251	57.383	64.230	70.415	76.364	82.392	88.392
1.0	0.001	0	17.322	21.731	25.425	31.632	39.308	45.870	53.560	60.437	68.230	75.415	82.653	89.653	96.453
1.1	0.0005	0	17.590	21.898	25.488	31.462	38.732	44.838	51.874	58.063	64.976	71.221	78.703	85.703	92.703
1.1	0.001	0	17.573	21.855	25.413	31.307	38.419	44.325	51.031	56.823	63.147	68.703	75.703	82.703	89.703
1.3	0.0005	0	13.151	16.302	18.936	23.328	28.681	33.182	38.371	42.936	48.038	52.646	57.436	62.436	67.470
1.3	0.001	0	13.058	16.127	18.664	22.821	27.739	31.716	36.086	39.702	43.385	46.470	50.385	54.385	58.014
1.5	0.0005	0	9.839	12.296	14.269	17.562	21.580	24.958	28.855	32.284	36.115	39.578	43.741	47.751	51.692
1.5	0.001	0	9.851	12.133	14.015	17.091	20.702	23.591	26.714	29.238	31.751	33.674	37.461	40.461	44.461
		$X_0 = 0.1$													$r_a^2 = 0.25$

TABLE 18

 $\frac{\mu b \omega_a}{a}$  FOR BENDING-TORSION FLUTTER

$\left(\frac{\omega_h}{\omega_a}\right)$	$\mu_M$	$\theta/\mu$	600									
			40	60	80	120	180	240	320	400	500	600
0	0.0005 0.001	0 -	*	*	*	*	*	*	*	*	*	*
0.3	0.0005 0.001	0 -	*	*	*	*	*	*	*	*	*	*
0.5	0.0005 0.001	0 -	*	*	*	*	*	*	*	*	*	*
0.7	0.0005 0.001	0 -	*	*	*	*	*	*	*	*	*	*
0.8	0.0005 0.001	0 -	*	*	*	*	*	*	*	*	*	*
0.9	0.0005 0.001	0 -	*	*	*	*	*	*	*	*	*	*
1.0	0.0005 0.001	0 -	*	*	*	*	*	*	*	*	*	*
1.1	0.0005 0.001	0 -	*	*	*	*	*	*	*	*	*	*
1.3	0.0005 0.001	0 -	*	*	*	*	*	*	*	*	*	*
1.5	0.0005 0.001	0 -	*	*	*	*	*	*	*	*	*	*

$$X_a = 0.1 \quad X_0 = 0.4 \quad r_a^2 = 0.09$$

TABLE 19  $\frac{\mu_M}{\theta}$  FOR BENDING-TORSION FLUTTER

WADC TN 57-310

$\frac{M_h}{M_0}$	$\frac{M_h}{M_0} \cdot \frac{1}{r^2}$	40	60	80	120	180	240	320	400	500	600
0	0	*	*	*	*	*	*	*	*	*	*
0	0.0005	-	-	-	-	-	-	-	-	-	-
0	0.001	-	-	-	-	-	-	-	-	-	-
0.3	0	*	*	*	*	*	*	*	*	*	*
0.3	0.0005	-	-	-	-	-	-	-	-	-	-
0.3	0.001	-	-	-	-	-	-	-	-	-	-
0.5	0	*	*	*	*	*	*	*	*	*	*
0.5	0.0005	-	-	-	-	-	-	-	-	-	-
0.5	0.001	1.092	3.698	5.624	9.162	14.263	19.293	25.963	32.616	40.925	49.233
0.7	0	*	*	*	*	*	*	*	*	*	*
0.7	0.0005	-	-	-	-	-	-	-	-	-	-
0.7	0.001	-	-	-	-	-	-	-	-	-	-
0.8	0	*	*	*	*	*	*	*	*	*	*
0.8	0.0005	-	-	-	-	-	-	-	-	-	-
0.8	0.001	12.097	15.402	18.225	23.111	29.442	35.136	42.167	48.793	56.685	64.293
0.9	0	*	*	*	*	*	*	*	*	*	*
0.9	0.0005	-	-	-	-	-	-	-	-	-	-
0.9	0.001	-	-	-	-	-	-	-	-	-	-
1.0	0	*	*	*	*	*	*	*	*	*	*
1.0	0.0005	-	-	-	-	-	-	-	-	-	-
1.0	0.001	-	-	-	-	-	-	-	-	-	-
1.1	0	*	*	*	*	*	*	*	*	*	*
1.1	0.0005	-	-	-	-	-	-	-	-	-	-
1.1	0.001	-	-	-	-	-	-	-	-	-	-
1.3	0	*	*	*	*	*	*	*	*	*	*
1.3	0.0005	-	-	-	-	-	-	-	-	-	-
1.3	0.001	-	-	-	-	-	-	-	-	-	-
1.5	0	*	*	*	*	*	*	*	*	*	*
1.5	0.0005	-	-	-	-	-	-	-	-	-	-
1.5	0.001	-	-	-	-	-	-	-	-	-	-

$$r_a^2 = 0.16$$

$$X_a = 0.1$$

$$r_a^2 = 0.16$$

$$X_a = 0.4$$

TABLE 20  
 $\frac{\mu_{b\alpha}}{q}$  FOR BENDING-TORSION FLUTTER

WADC TN 57-310

$(\frac{S_1}{C_1})$	$\frac{S_1}{C_1} \cdot \mu_M$	40	60	80	120	180	240	320	400	500	600
0	0.0005 0.001	*	*	*	*	*	*	*	*	*	*
0.3	0.0005 0.001	*	*	*	*	*	*	*	*	*	*
0.5	0.0005 0.001	-	-	-	-	-	-	-	-	-	-
0.7	0.0005 0.001	5.687 6.174 6.623	7.362 8.195 8.946	8.721 9.953 11.038	10.944 13.091 14.905	13.614 17.347 20.341	15.840 21.343 25.562	18.394 26.457 32.333	20.634 31.425 38.953	23.131 37.502 47.059	25.384 43.472 55.000
0.8	0.0005 0.001	9.946 10.287 10.614	12.556 13.158 13.724	14.711 15.614 16.450	18.273 19.878 21.313	22.587 25.428 27.855	26.200 30.443 33.919	30.356 36.652 41.558	34.004 42.516 48.841	38.079 49.522 57.591	41.758 56.265 66.029
0.9	0.0005 0.001	14.846 15.080 15.307	18.581 18.997 19.391	21.682 22.308 22.893	26.830 27.946 28.957	33.081 35.067 36.786	38.326 41.295 43.776	44.367 48.795 52.314	49.678 55.676 60.280	55.607 63.680 69.775	60.971 71.247 79.007
1.0	0.0005 0.001	18.137 18.225 18.308	22.602 22.753 22.894	26.319 26.544 26.749	32.503 32.896 33.239	40.025 40.712 41.277	46.343 47.356 48.151	53.620 55.107 56.223	60.022 62.013 63.492	67.171 69.825 71.909	73.629 76.979 80.058
1.1	0.0005 0.001	0 17.357 17.319 17.279	21.573 21.498 21.418	25.091 24.970 24.841	30.949 30.717 30.464	38.083 37.639 37.134	44.077 43.372 42.534	50.984 49.860 48.433	57.061 55.451 53.211	63.850 61.484 57.824	69.982 66.739 60.807
1.3	0.0005 0.001	12.349 12.247 12.143	15.306 15.116 14.921	17.777 17.482 17.176	21.898 21.349 20.766	26.922 25.896 24.762	31.146 29.539 27.674	36.015 33.481 30.297	40.300 36.665 31.620	45.088 39.818 31.215	49.413 42.195 27.321
1.5	0.0005 0.001	9.171 9.071 8.369	11.349 11.165 10.974	13.172 12.886 12.586	16.214 15.682 15.108	19.925 18.927 17.801	23.046 21.479 20.929	26.644 24.162 21.031	29.811 26.234 21.031	33.349 28.134 18.999	36.547 29.358 12.240

$$X_a = 0.1 \quad X_0 = 0.4 \quad r_a^2 = 0.25$$

TABLE 21  $\frac{\mu_b}{\mu_a}$  FOR BENDING-TORSION FLUTTER  
WADC TN 57-310 32

$\frac{W_h}{\alpha \mu}$	$\delta/\mu$	$\mu_M$	40	60	80	100	120	140	160	180	200	220	240	260	280	300	320	340	360	380	400	420	440	460	480	500	520	540	560	580	600
0	0.0005 0.001	0 0.0005 0.001	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	
0.3	0.0005 0.001	0 0.0005 0.001	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	
0.5	0.0005 0.001	0 0.0005 0.001	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-		
0.7	0.0005 0.001	0 0.0005 0.001	4.260	5.632	6.730	8.511	10.637	12.404	14.428	16.200	18.174	19.954																			
0.8	0.0005 0.001	0 0.0005 0.001																													
0.9	0.0005 0.001	0 0.0005 0.001																													
1.0	0.0005 0.001	0 0.0005 0.001																													
1.1	0.0005 0.001	0 0.0005 0.001																													
1.3	0.0005 0.001	0 0.0005 0.001																													
1.5	0.0005 0.001	0 0.0005 0.001																													

$r_a^2 = 0.36$

$X_0 = 0.4$

$X_a = 0.1$

TABLE 22  
WADC TN 57-310

$\frac{\mu_b e}{\alpha}$  FOR BENDING-TORSION FLUTTER

$(\frac{\omega_n}{\omega})$	$\frac{8}{\mu}$	$\frac{\mu M}{\mu}$	40	60	80	120	180	240	320	400	500	600
0	0.0005	1.422	*	*	*	*	*	*	*	*	*	*
	0.001	2.940	3.208	4.676	7.413	11.374	15.283	20.464	25.631	32.079	38.521	38.521
0.3	0.0005	4.369	5.673	6.729	8.453	10.523	12.247	14.226	15.960	17.894	19.638	54.527
	0.001	5.119	6.942	8.587	11.638	15.956	20.137	25.614	31.028	37.747	44.429	44.429
0.5	0.0005	8.881	11.173	13.068	16.208	20.014	23.204	26.874	30.101	33.702	36.954	56.453
	0.001	9.334	11.974	14.275	18.352	23.812	28.875	35.295	41.491	49.043	56.453	70.255
0.7	0.0005	14.395	17.976	20.953	25.901	31.916	36.965	42.779	47.893	53.603	58.762	58.762
	0.001	25.742	18.601	21.904	27.616	34.997	41.619	49.785	57.484	66.696	75.610	75.610
0.8	0.0005	16.907	21.077	24.548	30.323	37.346	43.241	50.038	56.005	62.677	68.705	68.705
	0.001	17.208	21.621	25.377	31.817	40.045	47.328	56.201	64.452	74.238	83.624	83.624
0.9	0.0005	18.367	22.871	26.624	32.866	40.462	46.848	54.201	60.679	67.884	74.412	74.412
	0.001	18.590	23.273	27.245	33.974	42.440	49.814	58.641	66.696	76.028	84.757	84.757
1.0	0.0005	18.402	22.894	26.640	32.874	40.463	46.838	54.184	60.647	67.865	74.386	74.386
	0.001	18.522	23.109	26.962	33.443	41.451	48.275	56.226	63.265	71.110	78.091	78.091
1.1	0.0005	17.367	21.594	25.119	30.989	38.136	44.140	51.059	57.147	63.946	70.089	70.089
	0.001	17.393	21.635	25.175	31.069	38.223	44.185	50.943	56.721	62.871	68.003	68.003
1.3	0.0005	17.412	21.656	25.188	31.028	37.967	43.500	49.223	53.210	55.434	53.236	53.236
	0.001	14.207	17.537	20.251	24.592	32.919	36.449	42.158	47.182	52.794	57.864	57.864
1.5	0.0005	11.813	14.668	17.052	21.023	25.862	29.927	34.614	38.737	43.343	47.504	47.504
	0.001	11.704	14.464	16.733	20.422	24.715	28.100	31.664	34.414	36.916	38.490	38.490

$$X_a = 0.1 \quad X_0 = 0.45 \quad r_a^2 = 0.09$$

TABLE 23 FOR BENDING-TORSION FLUTTER

WADC TN 57-310

$\frac{M}{\mu}$	$\frac{8}{\mu} \text{ HN}$	40	60	80	120	180	240	320	400	500	600
0	0.0005 0.001	1.153 2.384	2.602 4.070	3.793 5.639	6.012 8.679	9.225 13.163	12.395 17.617	16.597 23.540	20.787 29.453	26.017 36.840	27.221 44.223
0.3	0.0005 0.001	2.710 4.097	3.625 5.861	4.351 7.524	5.524 8.539	6.920 11.967	8.078 15.315	9.403 19.723	10.563 24.095	11.855 29.532	13.019 13.947
0.5	0.0005 0.001	6.019 6.462	7.619 8.394	8.937 10.094	11.113 13.152	13.746 17.318	15.949 21.239	18.484 26.267	20.710 31.160	23.194 37.158	25.437 43.065
0.7	0.0005 0.001	11.003 11.320	13.765 14.332	16.060 16.917	19.869 21.406	24.496 27.239	28.379 32.499	32.849 39.008	36.781 45.156	41.170 52.512	45.135 59.614
0.8	0.0005 0.001	14.346 14.882	17.900 18.390	20.858 21.600	25.774 27.110	31.753 34.151	36.771 40.389	42.555 47.990	47.633 55.061	53.310 63.431	58.438 71.440
0.9	0.0005 0.001	17.440 17.644	21.723 22.088	25.291 25.846	31.226 32.228	38.450 40.252	44.516 47.233	51.503 55.590	57.658 63.246	64.523 72.169	70.746 80.582
1.0	0.0005 0.001	18.675 18.756	23.277 23.417	27.135 27.340	33.607 33.947	41.574 42.113	49.641 49.051	54.721 56.234	61.247 63.237	68.536 71.106	75.121 78.225
1.1	0.0005 0.001	18.589 18.756	23.125 23.417	26.907 27.340	33.202 33.947	40.865 42.113	47.303 49.051	54.721 57.064	61.247 64.025	68.536 71.456	75.121 77.362
1.3	0.0005 0.001	18.675 18.762	23.277 25.685	27.135 31.753	33.607 35.763	41.574 49.051	48.346 52.507	54.721 64.025	61.247 67.590	68.536 71.905	75.121 77.362
1.5	0.0005 0.001	18.589 18.762	23.125 25.685	26.907 31.753	33.202 35.763	40.865 49.051	47.303 52.507	54.721 64.025	61.247 67.590	68.536 71.905	75.121 77.362

TABLE 24

WADDC TN 57-310

## $\frac{\mu b \omega_1}{\sigma}$ FOR BENDING-TORSION FLUTTER

$\left(\frac{\rho h}{\sigma g}\right)$	$\delta/\mu$	$\mu \alpha$	40	60	80	120	180	240	320	400	500	600
0	0.0005	0	*	*	*	*	*	*	*	*	*	*
	0.001	2.077	2.267	3.305	5.238	8.037	10.799	14.461	18.112	22.669	27.221	38.532
0.3	0.0005	1.919	2.656	3.229	4.143	5.223	6.115	7.133	8.022	9.012	9.903	29.992
	0.001	3.698	3.892	4.980	7.035	9.996	12.900	16.731	20.537	25.273	29.458	41.057
0.5	0.0005	0	1.919	2.656	3.229	4.143	5.223	6.115	7.133	8.022	9.012	9.903
	0.001	3.298	4.819	6.257	9.039	13.122	17.161	22.510	27.833	34.458	41.057	46.693
0.7	0.0005	0	4.590	5.844	6.873	8.568	10.615	12.327	14.293	16.020	17.947	19.686
	0.001	5.434	6.609	8.009	10.553	14.064	17.400	21.708	25.921	31.104	36.220	46.693
0.8	0.0005	0	8.932	11.195	13.072	16.185	19.955	23.135	26.785	29.983	33.576	36.811
	0.001	9.236	11.735	13.866	17.637	22.543	26.992	32.522	37.761	41.542	45.109	59.329
0.9	0.0005	0	12.426	15.518	18.090	22.363	27.558	31.918	36.936	41.350	46.281	50.734
	0.001	12.677	15.967	18.768	23.578	29.727	35.175	41.812	47.978	55.255	62.191	70.730
1.0	0.0005	0	16.576	20.652	24.048	29.696	36.568	42.340	48.994	54.832	61.383	67.267
	0.001	16.754	20.973	24.534	30.571	38.136	44.703	52.544	59.719	68.041	75.897	84.095
1.1	0.0005	0	18.742	23.312	27.123	33.467	41.191	47.679	55.155	61.733	69.079	75.716
	0.001	18.800	23.414	27.277	33.741	41.678	48.408	56.242	63.208	71.076	78.267	80.471
1.3	0.0005	0	16.976	21.090	24.523	30.242	37.207	43.060	49.806	55.741	62.370	68.360
	0.001	16.920	20.985	24.360	29.935	36.625	42.136	48.320	53.568	59.143	63.828	52.196
1.5	0.0005	0	11.428	14.174	16.469	20.294	24.956	28.875	33.392	37.367	41.807	45.819
	0.001	11.303	13.945	16.113	19.632	23.710	26.908	30.252	32.804	35.080	36.436	8.519

$X_a = 0.1$

$r_a^2 = 0.25$

TABLE 25  $\frac{\mu \alpha}{\sigma}$  FOR BENDING-TORSION FLUTTER  
WADC TN 57-310

$\frac{C_h}{\mu}$	$\delta/\mu$	$\mu_M$	40	60	80	120	180	240	320	400	500	600
0	0	*	*	*	*	*	*	*	*	*	*	*
0	0.0005 0.001											
0.3	0	1.478	2.123	2.613	3.387	4.293	5.040	5.89	6.631	7.455	8.197	
0.5	0	3.785	4.846	5.713	7.138	8.855	10.290	11.938	13.384	14.997	16.453	
0.7	0	7.648	9.601	11.218	13.899	17.153	19.881	23.020	25.781	28.862	31.645	
0.8	0	0	0	0	0	0	0	0	0	0	0	
0.9	0	0.0005 0.001										
1.0	0	0.0005 0.001										
1.1	0	0.0005 0.001										
1.3	0	0.0005 0.001										
1.5	0	0.0005 0.001										
	$X_a = 0.1$											
	$X_0 = 0.45$											
	$r_a^2 = 0.36$											

TABLE 26       $\frac{\mu_b \omega}{\omega_a}$  FOR BENDING-TORSION FLUTTER  
 WADC TN 57-310      37

$\frac{M_h}{M}$	$\frac{8/M}{\mu M}$	40	60	80	120	180	240	320	400	500	600
0	0.0005	7.088	8.824	10.249	12.643	15.557	18.007	20.829	23.312	26.085	28.591
	0.001	7.532	9.605	11.446	14.711	19.315	23.596	29.091	34.444	41.016	47.500
0.3	0.0005	7.952	10.336	12.525	16.618	22.424	28.041	35.381	42.619	51.573	60.454
	0.001	9.236	11.696	13.848	17.669	22.780	27.508	33.492	39.257	46.273	53.149
0.5	0.0005	9.609	12.351	14.823	19.361	25.668	31.684	39.465	47.083	56.456	65.714
	0.001	12.161	15.118	17.585	21.693	26.694	30.897	35.739	40.000	44.759	49.058
0.7	0.0005	12.497	15.723	18.505	23.349	29.667	35.380	42.471	49.194	57.270	65.102
	0.001	12.823	16.303	19.375	24.880	32.329	39.284	48.145	56.727	67.215	77.536
0.9	0.0005	17.105	21.264	24.733	30.511	37.546	43.456	50.267	56.259	62.953	69.000
	0.001	17.404	21.810	25.568	32.027	40.293	47.634	56.604	65.000	74.991	84.629
0.8	0.0005	19.255	23.937	27.842	34.348	42.265	48.923	56.596	63.330	70.864	77.672
	0.001	19.514	24.412	28.569	35.673	44.676	52.588	62.161	70.992	81.424	91.389
1.0	0.0005	19.769	24.874	29.273	36.936	46.920	55.972	67.237	78.020	91.302	104.880
	0.001	20.026	24.896	28.957	35.723	43.962	50.885	58.864	65.881	73.721	80.792
1.1	0.0005	20.196	25.206	29.430	36.578	45.491	53.179	62.257	70.464	79.808	88.387
	0.001	20.357	25.499	29.870	37.340	46.776	54.965	64.604	73.088	82.088	88.804
1.3	0.0005	19.149	23.805	27.689	34.157	42.032	48.648	56.273	62.982	70.475	77.245
	0.001	19.199	23.895	27.823	34.384	42.393	49.113	56.792	63.418	70.547	76.568
1.5	0.0005	19.240	23.962	27.910	34.480	42.378	48.763	55.480	60.258	63.021	60.397
	0.001	17.319	21.531	25.044	30.894	38.017	44.002	50.898	56.966	63.743	69.866
1.7	0.0005	17.273	21.412	24.902	30.612	37.436	43.004	49.142	54.183	59.232	63.034
	0.001	17.217	21.329	24.709	30.185	36.433	41.081	45.265	47.167	45.594	36.793
1.9	0.0005	13.513	16.799	19.539	24.104	29.661	34.330	39.711	44.445	49.733	54.510
	0.001	13.378	16.548	19.149	23.367	28.253	32.073	36.037	39.012	41.564	42.919
2.1	0.0005	13.235	16.276	18.714	22.504	26.468	28.971	30.381	30.490	23.873	-
	0.001	10.444	12.790	14.642	17.445	20.195	21.681	21.936	20.003	12.267	31.332

$$X_a = 0.1 \quad X_0 = 0.5 \quad r_a^2 = 0.09$$

TABLE 27 FOR BENDING-TORSION FLUTTER  
WADC TN 57-310

$\left(\frac{\omega_n}{\omega_0}\right)$	$\mu_M$	$\mu_F$	40	60	80	120	180	240	320	400	500	600
0	0	5.738	7.134	8.298	10.236	12.596	14.579	16.864	18.874	21.120	23.148	
	0.0005	6.096	7.772	9.259	11.945	15.611	19.060	23.480	27.781	33.052	38.244	
	0.001	6.433	8.358	10.124	13.423	18.093	22.601	28.476	34.255	41.386	48.438	
0.3	0	6.802	8.457	9.836	12.134	14.932	17.282	19.961	22.374	25.036	27.441	
	0.0005	7.131	9.044	10.723	13.717	17.740	21.475	26.214	30.786	36.354	41.810	
	0.001	7.443	9.591	11.535	15.117	20.114	24.887	31.061	37.100	44.517	51.828	
0.5	0	9.031	11.232	13.065	16.116	19.832	22.954	26.552	29.717	33.253	36.447	
	0.0005	9.325	11.752	13.852	17.530	22.356	26.745	32.216	37.417	43.675	49.746	
	0.001	9.604	12.245	14.589	18.814	24.564	29.951	36.819	43.462	51.552	59.473	
0.7	0	13.384	16.639	19.354	23.874	29.379	34.004	39.333	44.022	49.260	53.991	
	0.0005	13.636	17.093	20.046	25.124	31.629	37.406	44.459	51.043	58.847	66.329	
	0.001	13.882	17.532	20.706	26.293	33.675	40.426	48.887	56.979	66.795	76.436	
0.8	0	16.437	20.434	23.768	29.321	36.080	41.761	48.314	54.061	60.494	66.304	
	0.0005	16.665	20.849	24.402	30.469	38.163	44.928	53.104	60.671	69.598	78.129	
	0.001	16.889	21.252	25.013	31.563	40.109	47.845	57.505	66.735	78.093	89.590	
0.9	0	18.990	23.607	27.460	33.876	41.568	48.247	55.815	62.476	69.911	76.606	
	0.0005	19.158	23.916	27.929	34.731	43.241	50.611	59.402	67.402	76.741	85.497	
	0.001	19.322	24.214	28.384	35.547	44.694	52.807	62.721	72.019	83.275	94.572	
1.0	0	19.149	23.805	27.689	34.157	42.032	48.648	56.273	62.982	70.475	77.245	
	0.0005	19.193	23.886	27.811	34.372	42.399	49.166	56.968	63.800	71.333	77.960	
	0.001	19.233	23.955	27.909	34.519	42.567	49.252	56.685	62.683	68.048	70.106	
1.1	0	16.243	21.063	24.499	30.222	37.190	43.045	49.791	55.727	62.357	68.347	
	0.0005	16.868	20.925	24.284	29.813	36.396	41.751	47.640	52.477	57.341	61.046	
	0.001	16.788	20.770	24.034	29.303	35.297	39.767	43.852	45.850	44.749	37.045	
1.3	0	11.865	14.750	17.156	21.164	26.043	30.143	34.867	39.024	43.667	47.861	
	0.0005	11.704	14.453	16.697	20.307	24.424	27.573	30.736	32.976	34.671	35.200	
	0.001	11.537	14.140	16.201	19.340	22.468	24.225	24.693	22.765	14.576	-	
1.5	0	8.727	10.849	12.619	15.567	19.156	22.171	25.646	28.703	32.118	35.203	
	0.0005	8.562	10.547	12.152	14.695	17.153	19.568	21.468	22.594	23.025	22.356	
	0.001	8.392	10.228	11.648	13.718	15.541	16.188	15.285	11.606	-	-	

TABLE 28 FOR BENDING-TORSION FLUTTER

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$$X_a = 0.1 \quad X_0 = 0.5 \quad r_a^2 = 0.16$$

$\frac{M_1}{M}$	$\frac{M_2}{M}$	$\mu_M$	40	60	80	100	120	140	160	180	200	240	320	400	500	600
0	0	0	4.992	6.206	7.218	8.904	10.957	12.682	14.670	16.419	18.372	20.137				
	0.0005	0.001	5.301	6.757	8.049	10.380	13.558	16.544	20.367	24.081	28.625	33.094				
0.3	0	0	5.762	7.164	8.332	10.279	12.649	14.640	16.934	18.953	21.208	23.245				
	0.0005	0.001	6.053	7.683	9.117	11.676	15.122	18.327	22.394	26.320	31.097	35.776				
0.5	0	0	6.329	8.166	9.831	12.902	17.191	21.288	26.581	31.748	38.083	44.310				
	0.0005	0.001	7.455	9.267	10.779	13.297	16.363	18.939	21.907	24.519	27.436	30.071				
0.7	0	0	7.717	9.737	11.490	14.570	18.628	22.331	26.959	31.365	36.671	41.820				
	0.0005	0.001	7.969	10.180	12.149	15.712	20.578	25.144	30.968	36.594	43.434	50.112				
0.8	0	0	11.137	13.846	16.105	19.867	24.447	28.296	32.730	36.632	40.990	44.928				
	0.0005	0.001	11.361	14.247	16.715	20.963	26.411	31.254	37.164	42.677	49.197	55.428				
0.9	0	0	11.578	14.632	17.291	21.973	28.159	33.804	40.846	47.539	55.574	63.354				
	0.0005	0.001	14.497	18.133	21.219	26.485	33.150	38.996	46.037	52.537	60.158	67.392				
1.0	0	0	14.689	18.476	21.736	27.402	34.757	41.380	49.556	57.281	66.582	75.685				
	0.0005	0.001	17.940	22.303	25.941	32.003	39.381	45.576	52.734	59.008	66.053	72.395				
1.1	0	0	18.089	22.573	26.356	32.756	40.750	47.671	55.937	63.449	72.206	80.477				
	0.0005	0.001	18.236	22.840	26.762	33.490	42.077	49.703	59.049	67.884	78.713	89.801				
1.2	0	0	19.149	23.805	27.689	34.157	42.032	48.648	56.273	62.982	70.475	77.245				
	0.0005	0.001	19.187	23.876	27.798	34.355	42.388	49.181	57.058	64.025	71.834	78.888				
1.3	0	0	19.224	23.943	27.899	34.530	42.674	49.561	57.499	64.391	71.745	77.541				
	0.0005	0.001	19.224	23.943	27.899	34.530	42.674	49.561	57.499	64.391	71.745	77.541				
1.4	0	0	16.413	20.404	23.734	29.277	36.028	41.699	48.235	53.985	60.408	66.210				
	0.0005	0.001	16.328	20.249	23.492	28.826	35.170	40.327	46.001	50.673	55.401	59.050				
1.5	0	0	10.257	12.752	14.832	18.297	22.516	26.060	30.144	33.738	37.752	41.378				
	0.0005	0.001	10.093	12.450	14.366	17.427	20.874	23.454	25.952	27.592	28.581	32.401				
1.6	0	0	7.090	8.814	10.252	12.647	15.562	18.012	20.835	23.319	26.093	28.600				
	0.0005	0.001	6.925	8.511	9.784	11.775	13.915	15.392	16.604	17.082	16.676	14.984				
$X_a = 0.1 \quad X_0 = 0.5 \quad r_a^2 = 0.25$																

TABLE 29

 $\mu_{de}$  FOR BENDING-TORSION FLUTTER

WADC TN 57-310

$(\frac{\partial h}{\partial \alpha})$	$\frac{8/\mu}{\alpha}$	$\mu M$	40	60	80	120	180	240	320	400	500	600
0	0	4.535	5.638	6.558	8.090	9.955	11.522	13.328	14.917	16.691	18.295	
	0.0005 0.001											
0.3	0	5.156	6.410	7.456	9.197	11.318	13.099	15.152	16.959	18.976	20.799	
	0.0005 0.001											
0.5	0	6.551	8.143	9.472	11.685	14.379	16.642	19.251	21.546	24.109	26.425	
	0.0005 0.001											
0.7	0	9.757	12.130	14.109	17.404	21.417	24.789	28.674	32.092	35.910	39.359	
	0.0005 0.001											
0.8	0											
	0.0005 0.001											
0.9	0											
	0.0005 0.001											
1.0	0											
	0.0005 0.001											
1.1	0											
	0.0005 0.001											
1.3	0											
	0.0005 0.001											
1.5	0											
	0.0005 0.001											
$X_a = 0.1$			$X_0 = 0.5$			$r_a^2 = 0.36$						

TABLE 30  $\frac{\mu b_e}{d}$  FOR BENDING-TORSION FLUTTER  
WADC TN 57-310

TABLE 31  $\frac{\mu b \omega_a}{\sigma}$  FOR BENDING-TORSION FLUTTER

**WADC TN 57-310**

$\left(\frac{r_a^2}{c}\right)$	$\delta/\mu$	$\mu M$	40	60	80	120	180	240	320	400	500	600
0	0 0.0005 0.001	8.196	10.110	11.716	14.400	17.677	20.436	23.618	26.419	29.550	32.379	
0.3	0 0.0005 c. 001											
0.5	0 0.0005 0.001											
0.7	0 0.0005 0.001											
0.8	0 0.0005 0.001											
0.9	0 0.0005 0.001											
1.0	0 0.0005 0.001											
1.1	0 0.0005 0.001											
1.3	0 0.0005 0.001											
1.5	0 0.0005 0.001											

TABLE 32  
WADC TN 57-310

$\frac{\mu b a}{\rho}$  FOR BENDING-TORSION PLUTTER

TABLE 33  $\frac{\mu \text{lb}_\text{s}}{\text{in}}$  FOR BENDING-TORSION FLUTTER  
WADC TN 57-310 44

$\frac{\alpha h}{\delta}$	$\frac{\delta}{\mu}$	40	60	80	120	180	240	320	400	500	600
0	0	6.424	7.924	9.182	11.286	13.855	16.017	18.511	20.707	23.160	25.378
0	0.0005										
0	0.001										
0.3	0										
0.3	0.0005										
0.3	0.001										
0.5	0										
0.5	0.0005										
0.5	0.001										
0.7	0										
0.7	0.0005										
0.7	0.001										
0.8	0										
0.8	0.0005										
0.8	0.001										
0.9	0										
0.9	0.0005										
0.9	0.001										
1.0	0										
1.0	0.0005										
1.0	0.001										
1.1	0										
1.1	0.0005										
1.1	0.001										
1.3	0										
1.3	0.0005										
1.3	0.001										
1.5	0										
1.5	0.0005										
1.5	0.001										
$X_a = 0.1$		$X_0 = 0.55$		$r_a^2 = 0.36$							

TABLE 34  
WADC TN 57-310

$\frac{\mu b \omega}{d}$  FOR BENDING-TORSION FLUTTER

$\left(\frac{S_1}{S_2}\right)$	$8/\mu$	$\mu_M$	40	60	80	120	180	240	320	400	500	600
0	0	0	*	*	*	*	*	*	*	*	*	*
	0.0005	0.001	*	*	*	*	*	*	*	*	*	*
0.3	0	0.0005	*	*	*	*	*	*	*	*	*	*
	0.0005	0.001	-	1.833	4.306	8.191	13.617	18.935	25.974	32.995	41.766	50.542
0.5	0	0.0005	6.316	7.986	9.362	11.637	14.389	16.694	19.344	21.673	24.271	26.617
	0.0005	0.001	6.784	8.808	10.592	13.806	18.197	22.342	27.672	32.875	39.276	45.603
0.7	0	0.0005	7.222	9.559	11.692	15.674	21.325	26.802	33.973	41.058	49.845	58.583
	0.0005	0.001	9.522	11.848	13.788	17.016	20.945	24.246	28.049	31.394	35.131	38.507
0.8	0	0.0005	9.827	12.397	14.620	18.513	23.627	28.285	34.107	39.662	46.374	52.923
	0.0005	0.001	10.123	12.921	15.405	19.890	26.015	31.179	39.199	46.449	55.438	64.513
0.9	0	0.0005	0	0	0	0	0	0	0	0	0	0
1.0	0	0.0005	0	0	0	0	0	0	0	0	0	0
1.1	0	0.0005	0	0	0	0	0	0	0	0	0	0
1.3	0	0.0005	0	0	0	0	0	0	0	0	0	0
1.5	0	0.0005	0	0	0	0	0	0	0	0	0	0

TABLE 35  $\frac{\mu_{b\alpha}}{\alpha}$  FOR BENDING-TORSION FLUTTER  
WADC TN 57-310

$\frac{M}{\mu}$	$\frac{8}{\mu}$	$\mu M$	40	60	80	100	120	140	160	180	200	240	320	400	500	600
0	0	0.0005	0.001	0.0005	0.001	0.0005	0.001	0.0005	0.001	0.0005	0.001	0.0005	0.001	0.0005	0.001	0.0005
0.3	0	0.0005	0.001	0.0005	0.001	0	-	*	-	*	*	*	*	*	*	*
0.5	0	0.0005	0.001	0.0005	0.001	0.0005	0.001	0.0005	0.001	0.0005	0.001	0.0005	0.001	0.0005	0.001	0.0005
0.7	0	0.0005	0.001	0.0005	0.001	0	-	*	-	*	*	*	*	*	*	*
0.8	0	0.0005	0.001	0	0.0005	0.001	0	0.0005	0.001	0	0.0005	0.001	0	0.0005	0.001	0
0.9	0	0.0005	0.001	0	0.0005	0.001	0	0.0005	0.001	0	0.0005	0.001	0	0.0005	0.001	0
1.0	0	0.0005	0.001	0	0.0005	0.001	0	0.0005	0.001	0	0.0005	0.001	0	0.0005	0.001	0
1.1	0	0.0005	0.001	0	0.0005	0.001	0	0.0005	0.001	0	0.0005	0.001	0	0.0005	0.001	0
1.3	0	0.0005	0.001	0	0.0005	0.001	0	0.0005	0.001	0	0.0005	0.001	0	0.0005	0.001	0
1.5	0	0.0005	0.001	0	0.0005	0.001	0	0.0005	0.001	0	0.0005	0.001	0	0.0005	0.001	0

$r_a^2 = 0.16$

$X_0 = 0.35$

$X_a = 0.2$

TABLE 36  
WADC TN 57-310

$\frac{\mu b \omega}{\alpha}$  FOR BENDING-TORSION FLUTTER

$\frac{V_h}{\omega_a}$	$\mu_M$	40	60	80	100	120	140	160	180	200	240	320	400	500	600
0	0	*	*	*	*	*	*	*	*	*	*	*	*	*	*
0	0.0005	*	*	*	*	*	*	*	*	*	*	*	*	*	*
0	0.001	*	*	*	*	*	*	*	*	*	*	*	*	*	*
0.3	0	*	*	*	*	*	*	*	*	*	*	*	*	*	*
0.3	0.0005	-	-	-	-	-	-	-	-	-	-	-	-	-	-
0.3	0.001	*	*	*	*	*	*	*	*	*	*	*	*	*	*
0.5	0	2.033	2.877	3.524	4.550	5.756	6.750	7.883	8.872	9.971	10.961				
0.5	0.0005	2.793	4.073	5.214	7.342	10.380	13.343	17.242	21.107	25.912	30.693				
0.5	0.001	3.394	4.988	6.475	9.326	13.487	17.589	23.013	28.401	35.096	41.750				
0.7	0	7.403	9.246	10.779	13.325	16.420	19.019	22.010	24.642	27.580	30.234				
0.7	0.0005	7.683	9.744	11.530	14.666	18.799	22.572	27.288	31.776	37.173	42.400				
0.7	0.001	7.950	10.212	12.223	15.860	20.823	25.473	31.386	37.074	43.946	50.608				
0.8	0	*	*	*	*	*	*	*	*	*	*	*	*	*	*
0.8	0.0005	*	*	*	*	*	*	*	*	*	*	*	*	*	*
0.8	0.001	*	*	*	*	*	*	*	*	*	*	*	*	*	*
0.9	0	*	*	*	*	*	*	*	*	*	*	*	*	*	*
0.9	0.0005	*	*	*	*	*	*	*	*	*	*	*	*	*	*
0.9	0.001	*	*	*	*	*	*	*	*	*	*	*	*	*	*
1.0	0	*	*	*	*	*	*	*	*	*	*	*	*	*	*
1.0	0.0005	*	*	*	*	*	*	*	*	*	*	*	*	*	*
1.0	0.001	*	*	*	*	*	*	*	*	*	*	*	*	*	*
1.1	0	*	*	*	*	*	*	*	*	*	*	*	*	*	*
1.1	0.0005	*	*	*	*	*	*	*	*	*	*	*	*	*	*
1.1	0.001	*	*	*	*	*	*	*	*	*	*	*	*	*	*
1.3	0	*	*	*	*	*	*	*	*	*	*	*	*	*	*
1.3	0.0005	*	*	*	*	*	*	*	*	*	*	*	*	*	*
1.3	0.001	*	*	*	*	*	*	*	*	*	*	*	*	*	*
1.5	0	*	*	*	*	*	*	*	*	*	*	*	*	*	*
1.5	0.0005	*	*	*	*	*	*	*	*	*	*	*	*	*	*
1.5	0.001	*	*	*	*	*	*	*	*	*	*	*	*	*	*

$r_a^2 = 0.25$

$X_0 = 0.35$

$\mu_{ba}$  FOR BENDING-TORSION FLUTTER

TABLE 37  
WADC TN 57-310

$\frac{\omega_h}{\omega_n}$	$\frac{\mu_M}{\mu}$	40	60	80	100	120	140	160	180	200	220	240	260	280	300	320	340	360	380	400	420	440	460	480	500	520	540	560
0	0 0.0005 0.001	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*
0.3	0 0.0005 0.001	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*
0.5	0 0.0005 0.001	-	0.876	1.472	2.229	3.028	3.656	4.355	4.956	5.618	6.210																	
0.7	0 0.0005 0.001	6.708	8.394	9.793	12.117	14.939	17.307	20.034	22.431	25.109	27.527																	
0.8	0 0.0005 0.001	0																										
0.9	0 0.0005 0.001	0																										
1.0	0 0.0005 0.001	0																										
1.1	0 0.0005 0.001	0																										
1.3	0 0.0005 0.001	0																										
1.5	0 0.0005 0.001	0																										
		$X_a = 0.2$																										$r_a^2 = 0.36$

TABLE 38 FOR BENDING-TORSION FLUTTER  
WADC TN 57-310

TABLE 39  $\frac{\mu b \omega_s}{\sigma}$  FOR BENDING-TORSION FLUTTER

$\left(\frac{C_1}{C_2}\right)$	$\mu_M$	$\mu_N$	40	60	80	100	120	140	160	180	200	240	320	400	500	600
0	0	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*
	0.0005	1.117	2.520	3.673	5.822	8.934	12.004	16.074	20.132	25.196	28.525	35.678	30.256	35.678	42.828	
0.3	0	3.889	4.955	5.828	7.268	9.006	10.459	12.128	13.594	15.229	16.705	20.452	24.652	29.852	35.014	
	0.0005	4.404	5.844	7.144	9.548	12.931	16.194	20.452	24.652	29.852	35.014	39.177	46.327	46.327	46.327	
0.5	0	7.273	9.058	10.546	13.021	16.032	18.561	21.475	24.038	26.900	29.486	32.068	37.727	43.255	43.255	
	0.0005	7.583	9.613	11.384	14.519	18.597	22.546	27.403	32.068	37.727	43.255	45.650	52.985	52.985	52.985	
0.7	0	10.499	13.005	15.101	18.597	22.860	26.444	30.577	34.213	38.277	41.948	40.528	46.878	52.992	52.992	
	0.0005	10.728	13.419	15.730	19.731	24.897	29.518	35.197	40.528	46.878	52.992	53.770	53.770	53.770	53.770	
0.8	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
	0.0005	0.001	0	0	0	0	0	0	0	0	0	0	0	0	0	
0.9	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
	0.0005	0.001	0	0	0	0	0	0	0	0	0	0	0	0	0	
1.0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
	0.0005	0.001	0	0	0	0	0	0	0	0	0	0	0	0	0	
1.1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
	0.0005	0.001	0	0	0	0	0	0	0	0	0	0	0	0	0	
1.3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
	0.0005	0.001	0	0	0	0	0	0	0	0	0	0	0	0	0	
1.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
	0.0005	0.001	0	0	0	0	0	0	0	0	0	0	0	0	0	

$X_a = 0.2$

$X_0 = 0.4$

$r_a^2 = 0.16$

TABLE 40  $\frac{\mu_{b\omega}}{\mu_N}$  FOR BENDING-TORSION FLUTTER  
WADC TN 57-310

$\frac{2h}{\mu}$	$\delta/\mu$	$\mu_M$	40	60	80	120	180	240	320	400	500	600
0	0	*	*	*	*	*	*	*	*	*	*	*
	0.0005	0.978	2.207	3.217	5.099	7.824	10.513	14.078	17.632	22.067	26.499	*
	0.001	2.022	3.452	4.783	7.362	11.165	14.943	19.966	24.982	31.248	37.510	*
0.3	0	2.955	3.807	4.500	5.636	7.003	8.143	9.452	10.601	11.881	13.037	*
	0.0005	3.472	4.687	5.790	7.848	10.772	13.610	17.328	21.004	25.562	30.091	*
	0.001	3.921	5.424	6.837	9.552	13.506	17.395	22.527	27.618	33.937	40.212	*
0.5	0	5.917	7.387	8.610	10.642	13.113	15.187	17.575	19.676	22.022	24.141	*
	0.0005	6.218	7.924	9.419	12.081	15.656	18.975	23.183	27.238	32.168	36.989	*
	0.001	6.504	8.422	10.155	13.342	17.782	22.013	27.469	32.783	39.279	45.642	*
0.7	0	9.443	11.705	13.595	16.747	20.590	23.821	27.545	30.823	34.485	37.793	*
	0.0005	9.651	12.078	14.162	17.766	22.413	26.562	31.645	36.401	42.039	47.438	*
	0.001	9.851	12.434	14.694	18.697	24.016	28.892	34.993	40.800	47.788	54.578	*
0.8	0	0	0	0	0	0	0	0	0	0	0	*
	0.0005	0	0	0	0	0	0	0	0	0	0	*
	0.001	0	0	0	0	0	0	0	0	0	0	*
0.9	0	0	0	0	0	0	0	0	0	0	0	*
	0.0005	0	0	0	0	0	0	0	0	0	0	*
	0.001	0	0	0	0	0	0	0	0	0	0	*
1.0	0	0	0	0	0	0	0	0	0	0	0	*
	0.0005	0	0	0	0	0	0	0	0	0	0	*
	0.001	0	0	0	0	0	0	0	0	0	0	*
1.1	0	0	0	0	0	0	0	0	0	0	0	*
	0.0005	0	0	0	0	0	0	0	0	0	0	*
	0.001	0	0	0	0	0	0	0	0	0	0	*
1.3	0	0	0	0	0	0	0	0	0	0	0	*
	0.0005	0	0	0	0	0	0	0	0	0	0	*
	0.001	0	0	0	0	0	0	0	0	0	0	*
1.5	0	0	0	0	0	0	0	0	0	0	0	*
	0.0005	0	0	0	0	0	0	0	0	0	0	*
	0.001	0	0	0	0	0	0	0	0	0	0	*

$X_a = 0.2$

$X_0 = 0.4$

$r_a^2 = 0.25$

TABLE 41 FOR BENDING-TORSION FLUTTER  
WADC TN 57-310

TABLE 42  $\frac{\mu b \omega_1}{\sigma}$  FOR BENDING-TORSION FLUTTER  
WADC TN 57-310 53

$\frac{c_0}{c_a}$	$\delta/\mu$	$\mu_{\text{bf}}$	40	60	80	120	180	240	320	400	500	600
0	0	6.832	8.493	9.879	12.186	14.996	17.357	20.077	22.471	25.144	27.559	27.559
	0.0005	7.262	9.261	11.037	14.247	18.636	22.773	28.087	33.263	39.636	45.923	45.923
	0.001	7.668	9.969	12.083	16.038	21.655	27.095	34.212	41.240	49.947	58.595	58.595
0.3	0	9.263	11.475	13.324	16.409	20.170	23.333	26.979	30.188	33.773	37.013	37.013
	0.0005	9.598	12.078	14.240	18.055	23.114	27.759	33.602	39.203	45.996	52.635	52.635
	0.001	9.921	12.650	15.096	19.554	25.700	31.528	39.040	46.379	55.404	64.320	64.320
0.5	0	12.177	15.053	17.462	21.484	26.392	30.520	35.281	39.472	44.155	48.387	48.387
	0.0005	12.454	15.557	18.231	22.877	28.907	34.334	41.042	47.384	54.992	62.373	62.373
	0.001	12.725	16.044	18.968	24.189	31.219	37.767	46.114	54.229	64.228	74.205	74.205
0.7	0	13.967	17.248	19.998	24.592	30.199	34.918	40.360	45.181	50.505	55.343	55.343
	0.0005	14.201	17.675	20.652	25.782	32.360	38.209	45.363	52.063	60.046	67.758	67.758
	0.001	14.431	18.092	21.286	26.922	34.399	41.283	50.004	58.495	69.115	80.141	80.141
0.8	0	0	0	0	0	0	0	0	0	0	0	0
	0.0005	0	0	0	0	0	0	0	0	0	0	0
	0.001	0	0	0	0	0	0	0	0	0	0	0
0.9	0	0	0	0	0	0	0	0	0	0	0	0
	0.0005	0	0	0	0	0	0	0	0	0	0	0
	0.001	0	0	0	0	0	0	0	0	0	0	0
1.0	0	0	0	0	0	0	0	0	0	0	0	0
	0.0005	0	0	0	0	0	0	0	0	0	0	0
	0.001	0	0	0	0	0	0	0	0	0	0	0
1.1	0	0	0	0	0	0	0	0	0	0	0	0
	0.0005	0	0	0	0	0	0	0	0	0	0	0
	0.001	0	0	0	0	0	0	0	0	0	0	0
1.3	0	0	0	0	0	0	0	0	0	0	0	0
	0.0005	0	0	0	0	0	0	0	0	0	0	0
	0.001	0	0	0	0	0	0	0	0	0	0	0
1.5	0	0	0	0	0	0	0	0	0	0	0	0
	0.0005	0	0	0	0	0	0	0	0	0	0	0
	0.001	0	0	0	0	0	0	0	0	0	0	0

$X_0 = 0.45$        $X_0 = 0.2$        $r_a^2 = 0.09$

TABLE 43       $\frac{\mu_{\text{bf}}}{\mu_{\text{bf}} - \mu_{\text{bf}}^0}$  FOR BENDING-TORSION FLUTTER  
WADC TN 57-310

$\frac{C_1}{C_2}$	$\theta/\mu$	$\mu_M$	40	60	80	100	120	180	240	320	400	500	600
0	0	5.561	6.913	8.041	9.920	12.207	14.129	16.343	18.291	20.467	22.433		
	0.0005	5.909	7.534	8.973	11.582	15.139	18.488	22.783	26.963	32.091	37.144		
	0.001	6.236	8.104	9.818	13.021	17.558	21.942	27.661	33.293	40.248	47.136		
0.3	0	7.102	8.804	10.227	12.599	15.491	17.922	20.724	23.190	25.945	28.434		
	0.0005	7.390	9.321	11.010	14.002	17.990	21.665	26.301	30.753	36.155	41.434		
	0.001	7.666	9.808	11.735	15.260	20.141	24.775	30.747	36.718	43.159	50.750		
0.5	0	9.544	11.806	13.699	16.859	20.714	23.957	27.696	30.987	34.664	37.987		
	0.0005	9.778	12.229	14.342	18.020	22.799	27.102	32.418	37.436	43.437	49.233		
	0.001	10.006	12.634	14.951	19.093	24.664	29.835	36.387	42.698	50.374	57.895		
0.7	0	12.272	15.158	17.578	21.619	26.551	30.701	35.487	39.701	44.409	48.663		
	0.0005	12.466	15.512	18.118	22.600	28.326	33.396	39.570	45.323	52.140	58.684		
	0.001	12.657	15.856	18.639	23.530	29.977	35.867	43.263	50.383	59.140	67.966		
0.8	0	0.0005	0	0	0	0	0	0	0	0	0		
	0.0005	0	0	0	0	0	0	0	0	0	0		
	0.001	0	0	0	0	0	0	0	0	0	0		
0.9	0	0.0005	0	0	0	0	0	0	0	0	0		
	0.001	0	0	0	0	0	0	0	0	0	0		
	0.005	0	0	0	0	0	0	0	0	0	0		
1.0	0	0.0005	0	0	0	0	0	0	0	0	0		
	0.001	0	0	0	0	0	0	0	0	0	0		
	0.005	0	0	0	0	0	0	0	0	0	0		
1.1	0	0.0005	0	0	0	0	0	0	0	0	0		
	0.001	0	0	0	0	0	0	0	0	0	0		
	0.005	0	0	0	0	0	0	0	0	0	0		
1.3	0	0.0005	0	0	0	0	0	0	0	0	0		
	0.001	0	0	0	0	0	0	0	0	0	0		
	0.005	0	0	0	0	0	0	0	0	0	0		
1.5	0	0.0005	0	0	0	0	0	0	0	0	0		
	0.001	0	0	0	0	0	0	0	0	0	0		
	0.005	0	0	0	0	0	0	0	0	0	0		

$x_a = 0.2 \quad x_0 = 0.45 \quad r_a^2 = 0.16$

TABLE 44 FOR BENDING-TORSION FLUTTER  
WADC TN 57-310

$(\frac{M}{\rho A})$	$\delta/\mu$	$\mu M$	40	60	80	120	180	240	320	400	500	600
0	0	4.862	6.044	7.030	8.672	10.672	12.352	14.288	15.991	17.894	19.612	
	0.0005	5.164	6.582	7.841	10.113	13.211	16.124	19.853	23.478	27.916	32.282	
0.3	0	5.447	7.076	8.569	11.355	15.294	19.091	24.032	28.883	34.858	40.755	
	0.0005	6.258	7.905	9.347	11.908	15.329	18.489	22.478	26.311	30.259	35.498	
0.5	0	6.506	8.339	9.992	13.023	17.223	21.212	26.346	31.344	37.459	43.461	
	0.0005	8.047	9.958	11.557	14.226	17.482	20.220	23.377	26.155	29.260	32.065	
0.7	0	8.257	10.337	12.133	15.261	19.334	23.005	27.542	31.822	36.936	41.864	
	0.0005	8.461	10.698	12.673	16.206	20.961	25.369	30.939	36.283	42.746	49.033	
0.8	0	11.003	13.595	15.767	19.394	23.820	27.544	31.839	35.620	39.844	43.662	
	0.0005	11.169	13.894	16.223	20.218	25.304	29.791	35.226	40.262	46.189	51.834	
0.9	0	11.330	14.183	16.658	20.989	26.658	31.791	38.168	44.220	51.520	58.668	
	0.0005	0	0	0	0	0	0	0	0	0	0	
1.0	0	0	0	0	0	0	0	0	0	0	0	
	0.0005	0	0	0	0	0	0	0	0	0	0	
1.1	0	0	0	0	0	0	0	0	0	0	0	
	0.0005	0	0	0	0	0	0	0	0	0	0	
1.3	0	0	0	0	0	0	0	0	0	0	0	
	0.0005	0	0	0	0	0	0	0	0	0	0	
1.5	0	0	0	0	0	0	0	0	0	0	0	
	0.0005	0	0	0	0	0	0	0	0	0	0	
												$r_a^2 = 0.25$
												$x_0 = 0.45$

TABLE 45  $\frac{\mu_{b-a}}{\mu}$  FOR BENDING-TORSION FLUTTER  
WADC TN 57-310

$\left(\frac{\rho h}{\mu}\right)$	$\theta/\mu$	$\mu^M$	40	60	80	120	180	240	320	400	500	600
0	0 0.0005 0.001	0 4.436 5.515	6.414	7.913	9.737	11.270	13.036	14.590	16.326	17.895		
0.3	0 0.0005 0.001	0 5.361 6.650	7.728	9.523	11.712	13.551	15.671	17.537	19.621	21.504		
0.5	0 0.0005 0.001	0 7.260 8.842	10.264	12.636	15.529	17.963	20.768	23.237	25.996	28.488		
0.7	0 0.0005 0.001	0 10.101 12.483	14.478	17.810	21.876	25.297	29.242	32.715	36.596	40.103		
0.8	0 0.0005 0.001	0 13.101 15.483	17.478	20.810	24.876	28.297	32.242	35.715	39.596	43.103		
0.9	0 0.0005 0.001	0 16.101 18.483	19.478	22.810	26.876	30.297	34.242	37.715	41.596	45.103		
1.0	0 0.0005 0.001	0 19.101 21.483	22.478	25.810	29.876	33.297	37.242	40.715	44.596	48.103		
1.1	0 0.0005 0.001	0 22.101 24.483	25.478	28.810	32.876	36.297	40.242	43.715	47.596	51.103		
1.3	0 0.0005 0.001	0 26.101 28.483	29.478	32.810	36.876	40.297	44.242	47.715	51.596	55.103		
1.5	0 0.0005 0.001	0 30.101 32.483	33.478	36.810	40.876	44.297	48.242	51.715	55.596	59.103		

$$X_a = 0.2 \quad X_0 = 0.45 \quad r_a^2 = 0.36$$

TABLE 46  
WADC TN 57-310

$\frac{\mu_b}{\mu}$  FOR BENDING-TORSION FLUTTER

$\frac{\partial h}{\partial \alpha}$	$\theta/\mu$	$\mu M$	40	60	80	120	180	240	320	400	500	600
0	0	9.828	12.124	14.049	17.268	21.198	24.506	28.322	31.682	35.436	38.829	
	0.0005	10.124	12.659	14.864	18.737	23.837	28.485	34.296	39.838	46.529	53.048	
	0.001	10.410	13.170	15.633	20.091	26.191	31.936	39.306	46.481	55.284	63.966	
0.3	0	11.769	14.518	16.824	20.678	25.384	29.346	33.915	37.938	42.433	46.497	
	0.0005	12.035	15.000	17.559	22.010	27.788	32.986	39.406	45.467	52.724	59.744	
	0.001	12.294	15.466	18.263	23.259	29.982	36.230	44.165	51.831	61.188	70.386	
0.5	0	14.380	17.739	20.556	25.265	31.016	35.856	41.439	46.355	51.848	56.812	
	0.0005	14.629	18.194	21.253	26.534	33.320	39.366	46.775	53.726	62.015	70.020	
	0.001	14.875	18.638	21.929	27.751	35.496	42.640	51.690	60.463	71.281	82.130	
0.7	0	15.858	19.563	22.670	27.863	34.205	39.542	45.699	51.120	57.178	62.653	
	0.0005	16.076	19.962	23.283	28.984	36.249	42.667	50.469	57.735	66.349	74.636	
	0.001	16.291	20.354	23.883	30.071	38.211	45.649	55.014	64.089	75.398	87.123	
0.8	0	0	0	0	0	0	0	0	0	0	0	
	0.0005	0	0	0	0	0	0	0	0	0	0	
	0.001	0	0	0	0	0	0	0	0	0	0	
0.9	0	0	0	0	0	0	0	0	0	0	0	
	0.0005	0	0	0	0	0	0	0	0	0	0	
	0.001	0	0	0	0	0	0	0	0	0	0	
1.0	0	0	0	0	0	0	0	0	0	0	0	
	0.0005	0	0	0	0	0	0	0	0	0	0	
	0.001	0	0	0	0	0	0	0	0	0	0	
1.1	0	0	0	0	0	0	0	0	0	0	0	
	0.0005	0	0	0	0	0	0	0	0	0	0	
	0.001	0	0	0	0	0	0	0	0	0	0	
1.3	0	0	0	0	0	0	0	0	0	0	0	
	0.0005	0	0	0	0	0	0	0	0	0	0	
	0.001	0	0	0	0	0	0	0	0	0	0	
1.5	0	0	0	0	0	0	0	0	0	0	0	
	0.0005	0	0	0	0	0	0	0	0	0	0	
	0.001	0	0	0	0	0	0	0	0	0	0	

 $r_a^2 = 0.09$  $x_0 = 0.5$  $x_a = 0.2$ TABLE 47  
WADC TN 57-310 $\frac{\mu b}{\theta}$  FOR BENDING-TORSION FLUTTER

$\frac{\rho_1}{\rho_2}$	$\delta/\mu$	$\mu_M$	40	60	80	120	180	240	320	400	500	600
0	0	7.957	9.816	11.375	13.981	17.163	19.841	22.931	25.651	28.690	31.438	
	0.0005	8.190	10.237	12.015	15.135	19.232	22.958	27.602	32.020	37.338	42.504	
	0.001	8.415	10.638	12.618	16.192	21.065	25.636	31.475	37.136	44.053	50.848	
0.3	0	9.189	11.336	13.136	16.145	19.820	22.913	26.481	29.622	33.132	36.304	
	0.0005	9.402	11.722	13.724	17.208	21.731	25.800	30.822	35.557	41.217	46.680	
	0.001	9.610	12.092	14.282	18.194	23.451	28.327	34.500	40.444	47.667	54.734	
0.5	0	11.331	13.978	16.197	19.908	24.439	28.253	32.652	36.526	40.854	44.766	
	0.0005	11.524	14.328	16.733	20.880	26.197	30.919	36.683	42.064	48.443	54.561	
	0.001	11.713	14.669	17.249	21.798	27.813	33.328	40.238	46.851	54.866	62.714	
0.7	0	13.822	17.050	19.758	24.285	29.812	34.464	39.831	44.555	49.835	54.607	
	0.0005	13.999	17.374	20.254	25.190	31.462	36.986	43.681	49.898	57.250	64.304	
	0.001	14.173	17.692	20.740	26.069	33.051	39.404	47.377	55.077	64.621	74.384	
0.8	0	0	0	0	0	0	0	0	0	0	0	
	0.0005	0	0	0	0	0	0	0	0	0	0	
	0.001	0	0	0	0	0	0	0	0	0	0	
0.9	0	0	0	0	0	0	0	0	0	0	0	
	0.0005	0	0	0	0	0	0	0	0	0	0	
	0.001	0	0	0	0	0	0	0	0	0	0	
1.0	0	0	0	0	0	0	0	0	0	0	0	
	0.0005	0	0	0	0	0	0	0	0	0	0	
	0.001	0	0	0	0	0	0	0	0	0	0	
1.1	0	0	0	0	0	0	0	0	0	0	0	
	0.0005	0	0	0	0	0	0	0	0	0	0	
	0.001	0	0	0	0	0	0	0	0	0	0	
1.3	0	0	0	0	0	0	0	0	0	0	0	
	0.0005	0	0	0	0	0	0	0	0	0	0	
	0.001	0	0	0	0	0	0	0	0	0	0	
1.5	0	0	0	0	0	0	0	0	0	0	0	
	0.0005	0	0	0	0	0	0	0	0	0	0	
	0.001	0	0	0	0	0	0	0	0	0	0	

 $r_a^2 = 0.16$  $X_0 = 0.5$  $X_a = 0.2$ 

TABLE 48

 $\frac{\mu_{b\alpha}}{\mu}$  FOR BENDING-TORSION FLUTTER

$\frac{X_0}{\alpha}$	$\delta/\mu$	$\mu_{\text{bif}}$	40	60	80	100	120	140	160	180	200	240	320	400	500	600
0	0	6.922	8.539	9.895	12.162	14.930	17.260	19.948	23.176	24.958	27.348	36.610	32.208	37.740	43.456	
	0.0005	7.119	8.895	10.437	13.137	16.676	19.887	23.878	27.664	24.958	27.348					
	0.001	7.310	9.234	10.945	14.026	18.211	22.120	27.094	31.897	32.208	32.208					
0.3	0	7.837	9.668	11.203	13.769	16.904	19.541	22.584	25.263	28.257	30.963	39.688	35.073	40.379	46.279	
	0.0005	8.020	9.998	11.706	14.676	18.530	21.993	26.262	30.280	35.073	39.688					
	0.001	8.197	10.314	12.180	15.510	19.977	24.109	29.323	34.325	34.325	34.325					
0.5	0	9.604	11.847	13.728	16.873	20.714	23.946	27.675	30.958	34.627	37.942	45.920	40.833	45.869	52.236	
	0.0005	9.765	12.141	14.176	17.683	22.172	26.152	30.997	35.507	40.833	45.920					
	0.001	9.924	12.424	14.603	18.439	23.495	28.102	33.847	39.306	45.869	45.869					
0.7	0	12.283	15.152	17.558	21.581	26.493	30.627	35.396	39.594	44.286	48.527	56.016	50.045	55.391	63.068	
	0.0005	12.424	15.410	17.953	22.298	27.795	32.612	38.414	43.765	47.623	55.391					
	0.001	12.564	15.662	18.336	22.988	29.029	34.471	41.214	47.623	55.391	63.068					
0.8	0	0	0	0	0	0	0	0	0	0	0	$X_0 = 0.50$	$r_a^2 = 0.25$			
	0.0005	0	0	0	0	0	0	0	0	0	0					
	0.001	0	0	0	0	0	0	0	0	0	0					
0.9	0	0	0	0	0	0	0	0	0	0	0	$X_0 = 0.2$	$r_a^2 = 0.25$			
	0.0005	0	0	0	0	0	0	0	0	0	0					
	0.001	0	0	0	0	0	0	0	0	0	0					
1.0	0	0	0	0	0	0	0	0	0	0	0	$X_0 = 0.1$	$r_a^2 = 0.25$			
	0.0005	0	0	0	0	0	0	0	0	0	0					
	0.001	0	0	0	0	0	0	0	0	0	0					
1.1	0	0	0	0	0	0	0	0	0	0	0	$X_0 = 0.05$	$r_a^2 = 0.25$			
	0.0005	0	0	0	0	0	0	0	0	0	0					
	0.001	0	0	0	0	0	0	0	0	0	0					
1.3	0	0	0	0	0	0	0	0	0	0	0	$X_0 = 0.01$	$r_a^2 = 0.25$			
	0.0005	0	0	0	0	0	0	0	0	0	0					
	0.001	0	0	0	0	0	0	0	0	0	0					
1.5	0	0	0	0	0	0	0	0	0	0	0	$X_0 = 0.005$	$r_a^2 = 0.25$			
	0.0005	0	0	0	0	0	0	0	0	0	0					
	0.001	0	0	0	0	0	0	0	0	0	0					

TABLE 49

 $\frac{\mu_{\text{bif}}}{d}$  FOR BENDING-TORSION FLUTTER

WADC TN 57-310

$\left(\frac{\mu}{\mu_1}\right)$	$\theta/\mu$	$\mu_M$	40	60	80	120	180	240	320	400	500	600
0	0	6.289	7.758	8.990	11.049	13.564	15.681	18.123	20.273	22.675	24.846	
	0.0005											
	0.001											
0.3	0	7.037	8.681	10.060	12.365	15.179	17.548	20.280	22.686	25.374	27.804	
	0.0005											
	0.001											
0.5	0	8.560	10.559	12.236	15.040	18.463	21.344	24.667	27.593	30.863	33.818	
	0.0005											
	0.001											
0.7	0	11.196	13.812	16.005	19.671	24.149	27.917	32.264	36.092	40.369	44.234	
	0.0005											
	0.001											
0.8	0	0	0	0	0	0	0	0	0	0	0	
	0.0005											
	0.001											
0.9	0	0	0	0	0	0	0	0	0	0	0	
	0.0005											
	0.001											
1.0	0	0	0	0	0	0	0	0	0	0	0	
	0.0005											
	0.001											
1.1	0	0	0	0	0	0	0	0	0	0	0	
	0.0005											
	0.001											
1.3	0	0	0	0	0	0	0	0	0	0	0	
	0.0005											
	0.001											
1.5	0	0	0	0	0	0	0	0	0	0	0	
	0.0005											
	0.001											

$X_a = 0.2$        $X_0 = 0.50$        $r_a^2 = 0.36$

TABLE 50       $\frac{\mu_{be}}{\mu}$  FOR BENDING-TORSION FLUTTER  
WADC TN 57-310

$\omega_B/\omega_h$	$\delta/\mu$	$\mu M$	40	80	120	240	400
0	0	-	-	48.113 46.406	70.061 63.702	91.123 81.612	
	0.001	-	-	-	58.861 55.899	65.451 62.534	
0.3	0	-	-	-	73.290 66.918	95.421 85.645	
	0.001	-	-	-	61.500 58.792	68.482 65.677	
0.4	0	-	-	-	76.128 69.793	99.217 89.232	
	0.001	-	-	-	63.784 61.411	71.144 68.488	
0.5	0	-	-	-	80.295 74.111	104.831 94.588	
	0.001	-	-	-	66.991 65.488	75.037 72.727	
0.6	0	-	-	-	86.391 80.720	113.176 102.672	
	0.001	-	-	-	-	80.563 79.381	
0.7	0	-	-	-	95.354 91.774	126.136 115.605	
	0.001	-	-	-	-	-	
0.8	0	-	-	-	-	-	148.183 139.407
	0.001	-	-	-	-	-	
$x_1 = 0.8$		$x_B = 0.0$			$r_B^f = 0.00196$		

TABLE 51  $\frac{\mu b \omega_h}{\alpha}$  FOR BENDING-AILERON FLUTTER

No real solutions for values of  $\frac{\omega_B}{\omega_h}$  above 0.8 for the range of  $\mu M$  considered.

No Real Solutions

$$x_1 = 0.8 \quad x_2 = 0.01 \quad \omega^2 = 0.001, 96$$

TABLE 52  $\frac{\mu b \omega_n}{a}$  FOR BENDING-AILERON FLUTTER

No Real Solutions

$$x_1 = 0.8 \quad x_{\beta} = 0.014 \quad r_{\beta}^2 = 0.001,96$$

TABLE 53  $\frac{\mu b \omega_h}{a}$  FOR BENDING-AILERON FLUTTER

$\omega_B/\omega_h$	$\delta/\mu$	$\frac{\mu M}{\mu}$	40	80	120	240	400
0	0	-	31.061 29.342	38.738 35.271	55.484 49.222	71.943 63.254	
	0.001	-	29.287 28.470	35.730 33.320	46.716 43.101	51.752 48.396	
0.3	0	-	32.275 31.031	40.482 37.089	58.094 51.660	75.367 66.352	
	0.001	-	-	37.305 35.070	48.895 45.252	54.196 50.784	
0.4	0	-	-	42.004 38.724	60.398 53.830	78.395 69.105	
	0.001	-	-	38.664 36.657	50.816 47.170	56.355 52.909	
0.5	0	-	-	44.214 41.203	63.804 57.071	82.885 73.205	
	0.001	-	-	40.571 39.125	53.646 50.043	59.547 56.081	
0.6	0	-	-	47.339 45.098	68.862 61.969	89.581 79.375	
	0.001	-	-	-	57.822 54.409	64.287 60.875	
0.7	0	-	-	-	76.701 69.816	100.060 89.176	
	0.001	-	-	-	64.151 61.542	71.620 68.570	
0.8	0	-	-	-	89.955 84.334	118.330 106.827	
	0.001	-	-	-	-	-	-
0.9		-	-	-	-	-	158.176
	0.001	-	-	-	-	-	151.420
1.0	0	-	-	-	-	-	-
	0.001	-	-	-	-	-	-
$x_1 = 0.8$			$x_B = 0$			$r_B^2 = 0.00324$	

TABLE 54  $\frac{\mu b \omega_h}{\mu}$  FOR BENDING-AILERON FLUTTER  
 WADC TN 57-310

$\omega_\beta/\omega_h$	$\delta/\mu$	$\mu M$	40	80	120	240	400
0	0		24.927 18.570	35.735 25.860	43.952 31.518	62.415 44.362	80.708 57.164
	0.001		24.275 18.187	33.840 24.774	40.416 29.491	52.022 38.265	57.060 42.666
0.3	0		25.782 19.629	37.052 27.266	45.604 33.209	64.803 46.711	83.817 60.176
	0.001		25.110 19.220	35.091 26.112	41.943 31.058	54.030 40.253	59.286 44.847
0.4	0		26.381 20.651	38.030 28.598	46.847 34.802	66.620 48.916	86.191 62.998
	0.001		25.697 20.217	36.027 27.378	43.102 32.531	55.583 42.111	61.029 46.877
0.5	0		26.849 22.444	39.031 30.820	48.176 37.432	68.629 52.520	88.848 67.596
	0.001		26.161 21.965	37.001 29.485	44.369 34.955	57.368 45.130	63.095 50.150
0.6	0	-	38.013 36.116	47.890 42.974	68.938 59.671	89.528 76.560	
	0.001	-	36.057 34.548	44.233 40.043	57.962 51.042	64.157 56.389	
0.7	0	-	-	-	-	-	-
	0.001	-	-	-	-	-	-
0.8	0	-	-	-	-	-	-
	0.001	-	-	-	-	-	-
$x_1 = 0.8$		$x_\beta = 0.01$	$r_\beta^2 = 0.00324$				

TABLE 55  $\frac{\mu b \omega_h}{\alpha}$  FOR BENDING-AILERON FLUTTER

No real solutions for values of  $\frac{\omega_\beta}{\omega_h}$  above 0.8 for the range of  $\mu M$  considered

$\omega_b/\omega_h$	$\delta/\mu$	$\mu M$	40	80	120	240	400
0	0		23.049 19.606	33.366 27.035	41.137 32.871	58.539 46.169	75.755 59.447
	0.001		22.465 19.185	31.652 25.856	37.926 30.682	49.043 39.635	54.006 44.047
0.3	0	-		32.806 29.751	40.758 35.896	58.310 50.150	75.589 64.461
	0.001	-		31.159 28.430	37.654 33.457	49.049 42.929	54.232 47.549
0.4	0	-	-	-	-	-	-
	0.001	-	-	-	-	-	-
$x_1 = 0.8$			$x_B = 0.014$		$r_B^2 = 0.00324$		

TABLE 56       $\frac{\mu b \omega_h}{\alpha}$       FOR BENDING-AILERON FLUTTER  
 No real solutions for values of  $\frac{\omega_b}{\omega_h}$  above 0.4

$\frac{\omega_B}{\omega_a}$	$\frac{8}{\mu} \text{ } \mu\text{m}$	40	80	120	240	400
0	0	28.392 22.360	40.919 30.999	50.402 37.736	71.671 53.057	92.725 68.341
	0.001	27.730 22.036	38.988 30.213	46.788 36.257	60.953 48.451	68.050 56.781
	0	30.218 23.266	43.567 32.242	53.673 39.243	76.334 55.167	98.764 71.054
	0.001	29.519 22.968	41.521 31.398	49.838 37.659	64.946 50.256	72.538 58.774
0.3	0	31.854 24.076	45.948 33.348	56.616 40.583	80.533 57.041	104.204 73.463
	0.001	31.121 23.759	43.793 32.455	52.571 38.910	68.511 51.872	76.507 60.581
	0	34.313 25.292	49.540 35.000	61.060 42.581	86.880 59.833	112.429 77.049
	0.001	33.525 24.947	47.211 34.037	56.683 40.781	73.855 54.293	82.409 63.308
0.4	0	38.043 27.143	55.019 37.498	67.849 45.596	96.589 64.035	125.018 82.445
	0.001	37.166 26.756	52.409 36.430	62.934 43.608	81.942 57.957	91.256 67.457
	0	43.934 30.156	63.760 41.516	78.709 50.429	112.162 70.753	145.231 91.059
	0.001	42.903 29.703	60.664 40.283	72.866 48.146	94.722 63.829	105.077 74.123
0.5	0	53.483 36.007	78.366 49.098	97.000 59.479	138.573 83.241	179.600 107.029
	0.001	52.185 35.420	74.384 47.547	89.448 56.636	115.989 74.736	127.788 86.474
	0	58.777 42.325		108.905 68.437		
	0.001	57.349 41.580	83.081 54.841	100.237 65.016	130.108 85.328	142.933 98.374
0.6	0	:	:	:	154.383 128.525	202.980 162.901
	0.001	:	:	:	128.608 115.041	142.141 131.861
	$x_1 = 0.8$	$x_2 = 0$			$\zeta^2 = 0.001, 96$	

$x_0 = 0.4$

TABLE 57

$\frac{\mu_B \omega_a}{\omega_b} = 0.36$

FOR TORSION-AILERON PLUTTER

No real solutions at  $\frac{\omega_B}{\omega_a} = 1.0$

No real solutions

$x_1 = 0.8$	$x_3 = 0.01$	$r_3^2 = 0.001,96$
$x_0 = 0.4$		$r_\alpha^2 = 0.36$

TABLE 58  $\frac{\mu b \omega_a}{a}$  FOR TORSION-AILERON FLUTTER

No real solutions

$x_1 = 0.8$	$x_\beta = 0.014$	$r_\beta^2 = 0.001, 96$
$x_0 = 0.4$		$r_\alpha^2 = 0.36$

TABLE 59  $\frac{\mu b \omega_a}{a}$  FOR TORSION-AILERON FLUTTER

$\omega_B/\omega_a$	$\delta/\mu$	40	80	120	240	400
0	0	22.809 17.117	32.612 23.917	40.081 21.180	56.875 41.113	78.319 52.998
	0.001	22.290 16.926	31.110 23.367	37.276 28.141	48.587 37.851	54.503 44.754
0.3	0	24.283 17.772	34.731 24.825	42.689 30.285	60.582 42.664	78.319 54.996
	0.001	23.735 17.565	33.139 24.233	39.715 29.169	51.789 39.175	58.139 46.621
0.4	0	25.603 18.354	36.631 25.630	45.029 31.264	63.911 44.039	82.262 56.765
	0.001	25.027 18.134	34.955 25.003	41.895 30.083	54.637 40.359	61.339 47.530
0.5	0	27.584 19.222	39.488 26.827	48.551 32.717	68.922 46.078	89.110 59.389
	0.001	26.964 18.984	37.677 26.150	45.162 31.446	58.887 42.130	66.069 49.528
0.6	0	30.580 20.529	43.821 28.621	53.895 34.895	76.534 49.128	98.965 63.312
	0.001	29.887 20.264	41.792 27.873	50.095 33.492	65.268 44.798	73.097 52.561
0.7	0	35.279 22.616	50.657 31.469	62.342 38.342	88.582 53.948	114.573 69.507
	0.001	34.462 22.309	48.252 30.610	57.832 36.738	75.206 49.033	83.895 57.402
0.8	0	42.853 26.490	61.838 36.675	76.219 44.618	108.458 62.688	140.360 80.721
	0.001	41.813 26.105	58.748 35.617	70.409 42.654	91.232 56.731	100.999 66.220
0.85	0	47.407 30.278				
	0.001	46.227 29.815	65.357 40.369	78.414 48.222	101.466 63.929	111.796 74.463
0.9	0	-	69.280 53.496	86.653 64.132	124.814 89.017	162.229 114.129
	0.001	-	65.689 51.866	79.805 61.160	104.156 80.270	114.337 93.590
$x_1 = 0.8$		$x_B = 0$		$\frac{\delta}{\mu} = 0.003, 24$		

$x_1 = 0.4$   
TABLE 60

$\frac{\mu b \omega_a}{\omega}$

FOR TORSION-AILERON FLUTTER

No real solutions at  $\frac{\delta}{\omega_a} = 1.0$

$\omega_\beta/\omega_a$	$\delta/\mu$	$\mu M$	40	80	120	240	400
0	0	0	25.995 15.373	37.022 21.561	45.446 26.335	64.417 37.144	83.238 47.901
		0.001	25.339 15.146	35.124 20.917	41.909 25.132	54.037 33.491	59.704 39.088
0.3	0	0	26.587 16.226	37.912 22.728	46.557 27.750	66.017 39.124	85.318 50.447
		0.001	25.919 15.980	35.974 22.036	42.942 26.457	55.398 35.210	61.229 41.034
0.4	0	0	26.789 17.069	38.259 23.873	47.006 29.134	66.683 41.056	86.194 59.929
		0.001	26.123 16.805	36.318 23.132	43.382 27.754	56.024 36.889	61.977 42.936
0.5	0	0	26.397 18.592	37.851 25.900	46.561 31.569	66.128 44.437	85.514 57.262
		0.001	25.756 18.297	35.972 25.077	43.041 30.040	55.731 39.842	61.784 46.303
0.6	0	0	-	-	-	58.495 54.126	76.198 63.413
		0.001	-	-	-	-	-
$x_1 = 0.8$		$x_\beta = 0.01$	$r_\beta^2 = 0.003,24$				

$$x_0 = 0.4$$

$$r_\alpha^2 = 0.36$$

TABLE 61  $\frac{\mu b \omega_a}{a}$  FOR TORSION-AILERON FLUTTER

No real solutions for values of  $\frac{\omega_\beta}{\omega_a}$  above 0.6

$\omega_\beta/\omega_a$	$\delta/\mu$	$\mu M$	40	80	120	240	400
0	0		23.123 16.133	33.051 22.543	40.617 27.503	57.633 38.748	74.502 49.948
	0.001		22.576 15.869	31.452 21.804	37.627 26.130	48.814 34.624	54.403 40.127
0.3	0		21.763 17.992	31.421 24.890	38.717 30.286	55.071 42.565	71.256 54.819
	0.001		21.629 17.689	29.957 24.052	35.966 28.734	46.901 37.933	52.509 48.852
$x_1 = 0.8$			$x_\beta = 0.014$		$r_\beta^2 = 0.003,24$		
$x_0 = 0.4$					$r_\alpha^2 = 0.36$		

TABLE 62  $\frac{\mu b \omega_a}{a}$  FOR TORSION-AILERON FLUTTER

No real solutions for  $\frac{\omega_\beta}{\omega_a}$  above 0.3

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## APPENDIX

The use of the parameters  $\mu b \omega_a / a$  and  $\mu M$  to plot a flutter boundary enable one to plot the requirements of the aircraft and the flutter boundary on the same graph. For example, Fig. 2 shows the region

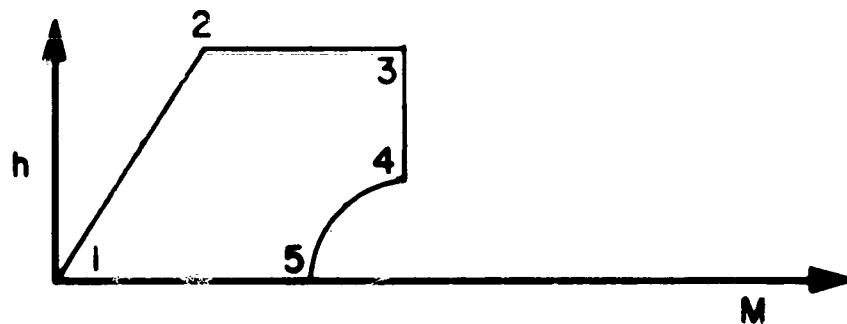


Fig. 2

Graph of Flight Capability of Typical Aircraft  
in Terms of Altitude and Mach Number

of expected flight capability for a typical aircraft on an altitude versus Mach number plot. After setting the wing configuration (which includes  $b$ ,  $\omega_a$  and  $m_0$ ) of the aircraft involved, Fig. 2 may be redrawn on a  $\mu b \omega_a / a$  versus  $\mu M$  plot and should look something like the sketch in Fig. 3.

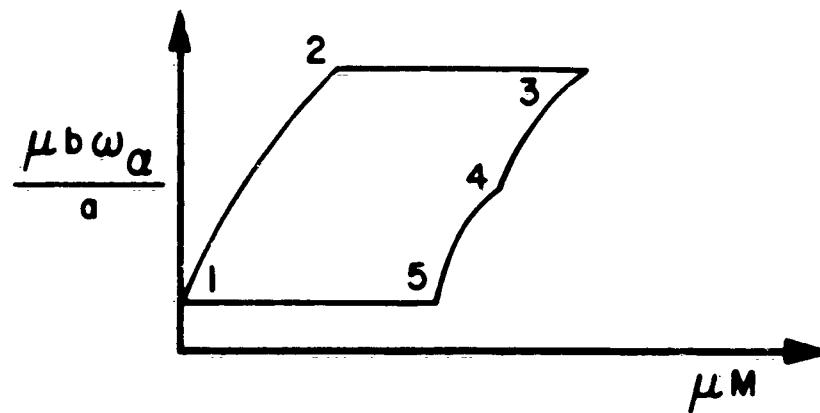


Fig. 3

Flight Capability of Typical Aircraft  
in Terms of  $\mu M$  and  $\mu b \omega_a / a$

Finally, if we superimpose the flutter boundary on the graph of Fig. 3, we will have a sketch similar to the one shown in Fig. 4. This diagram immediately

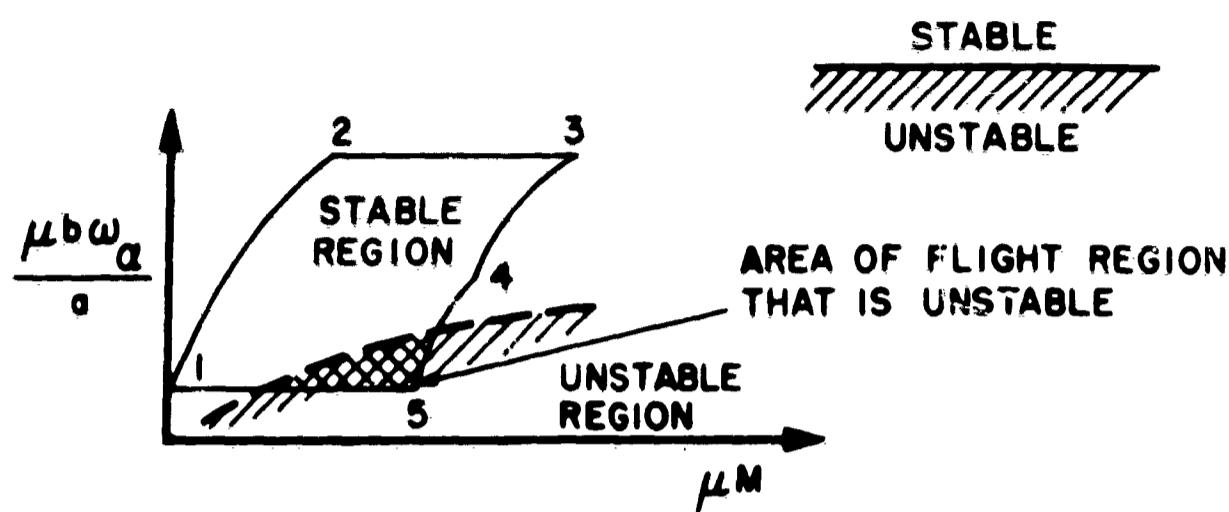


Fig. 4

Flutter Boundary Superimposed on Flight Boundary  
for Typical Aircraft in Terms of  $\mu M$  and  $\mu b\omega_a/a$ .

shows what part of the required flight region of the specific airplane configuration is unstable.